

Answers

Exercise 1.1

- (a) $2, \pi/3$ (b) $2, -2\pi/3$ (c) $2, -\pi/6$
(d) $2\sqrt{2}, 3\pi/4$ (e) $4, \pi/2$ (f) $6, -\pi/2$
- (a) $\sqrt{5} \operatorname{cis}(1.107)$ (b) $5 \operatorname{cis}(2.21)$
(c) $\operatorname{cis}(0.93)$ (d) $2 \operatorname{cis}(\pi/6)$ (e) $4 \operatorname{cis}(0)$
(f) $3 \operatorname{cis}(-\pi/2)$
- (a) $2i$ (b) $(3\sqrt{2}/2) - (3\sqrt{2}/2)i$
(c) $-\sqrt{3} + i$ (d) $-3i$ (e) $-1 + i$
(f) $-(5\sqrt{3}/2) + (5/2)i$
- (a) $2 - 3i, \sqrt{13} \operatorname{cis}(-0.98)$
(b) $-1 + 4i, \sqrt{17} \operatorname{cis}(1.82)$
(c) $3 + 5i, \sqrt{34} \operatorname{cis}(1.03)$
- (a) $a\sqrt{5}, 2$ (b) $\sqrt{(a^2 + 1)}, -a$
(c) $\sqrt{(a + 4)}, -2/a$ (d) $(1/a)\sqrt{(a + 1)}, a$

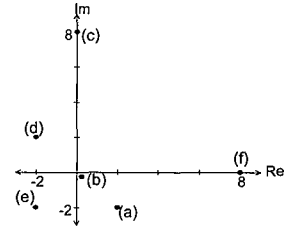
Exercise 1.2

- (a) $6 \operatorname{cis}(7\pi/12)$ (b) $9 \operatorname{cis}(-5\pi/6)$
(c) $20 \operatorname{cis}(-7\pi/12)$ (d) $10 \operatorname{cis}(5\pi/6)$
(e) $32 \operatorname{cis}(-3\pi/4)$ (f) $81 \operatorname{cis}(-2\pi/3)$
(g) $(1/81) \operatorname{cis}(2\pi/3)$ (h) $(1/64) \operatorname{cis}(\pi/2)$
- (a) $2 \operatorname{cis}(\pi/12)$ (b) $2 \operatorname{cis}(-\pi/12)$
(c) $2 \operatorname{cis}(-5\pi/6)$ (d) $\operatorname{cis}(\pi/2)$
(e) $\operatorname{cis}(2\pi/3)$ (f) $(1/3) \operatorname{cis}(-\pi/2)$
(g) $32 \operatorname{cis}(\pi/2)$ (h) $80 \operatorname{cis}(\pi)$
- (a) $1 - \sqrt{3}i, (1/4) - (\sqrt{3}/4)i$
(b) $(3\sqrt{2}/2) + (3\sqrt{2}/2)i, (\sqrt{2}/6) + (\sqrt{2}/6)i$
(c) $-2\sqrt{2} - 2\sqrt{2}i, (-\sqrt{2}/8) - (\sqrt{2}/8)i$
(d) $(5/2)(-\sqrt{3} + i), (-\sqrt{3}/10) + (1/10)i$
(e) $2, 1/2$ (f) $(1/2)i, 2i$
- (a) $8 \operatorname{cis}(-\pi/2), -8i$
(b) $4\sqrt{2} \operatorname{cis}(3\pi/4), -4 + 4i$
(c) $32 \operatorname{cis}(-\pi/3), 16 - 16\sqrt{3}i$
(d) $64 \operatorname{cis}(\pi), -64$
(e) $(1/64) \operatorname{cis}(0), 1/64$
(f) $(1/64) \operatorname{cis}(\pi), -1/64$
(g) $(1/32) \operatorname{cis}(5\pi/6), -(\sqrt{3})/64 + i/64$
(h) $(1/16) \operatorname{cis}(2\pi/3), -1/32 + (i\sqrt{3})/32$
- (a) $4\sqrt{2} \operatorname{cis}(-\pi/4), 4 - 4i$
(b) $4 \operatorname{cis}(\pi), -4$
(c) $2 \operatorname{cis}(2\pi/3), -1 + \sqrt{3}i$
(d) $27 \operatorname{cis}(\pi/2), 27i$
(e) $(1/2) \operatorname{cis}(-\pi/2), (-1/2)i$
(f) $(4/9) \operatorname{cis}(-5\pi/6), (2\sqrt{3}/9) - (2/9)i$
(g) $(ab/9) \operatorname{cis}(-\pi/4); (ab\sqrt{2})/18 - [(ab\sqrt{2})/18]i$
(h) $|a(5b)| \operatorname{cis}(3\pi/4);$
 $(-|a|\sqrt{2})/(10|b|) + [(|a|\sqrt{2})/(10|b|)]i$
- (a) $(2\sqrt{3}/3) \operatorname{cis}(\pi/6), 1 + (\sqrt{3}/3)i$
(b) $(16/9) \operatorname{cis}(-5\pi/6), (-8\sqrt{3}/9) - (8/9)i$
(c) $(8\sqrt{3}/3) \operatorname{cis}(-5\pi/6), -4 - (i4\sqrt{3})/3$
(d) $(1/16) \operatorname{cis}(\pi), -1/16$
(e) $(9\sqrt{3}/2) \operatorname{cis}(\pi/6), (27/4) + (9\sqrt{3}/4)i$

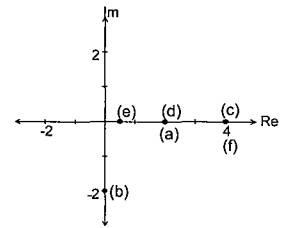
- (f) $(9\sqrt{3}/2) \operatorname{cis}(2\pi/3), (-9\sqrt{3}/4) + (27/4)i$
(g) $(1024/27) \operatorname{cis}(0), 1024/27$
(h) $(1024/27)^k \operatorname{cis}(0), (1024/27)^k$
- (a) $\bar{w} = a \operatorname{cis}(-\alpha), \bar{z} = b \operatorname{cis}(-\beta)$

Exercise 1.3

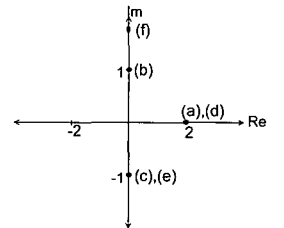
1.



2.

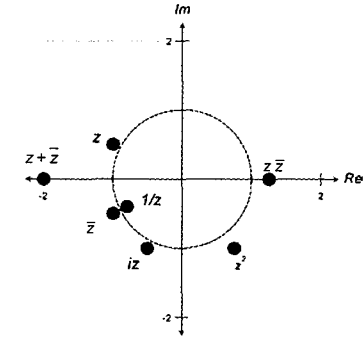


3.

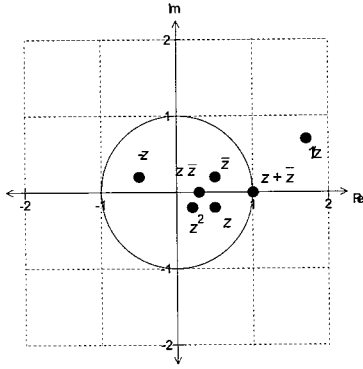


- (a) $r \operatorname{cis}(\theta - \pi)$ (b) $r \operatorname{cis}(-\theta)$
(c) $r \operatorname{cis}(\theta - \pi/2)$ (d) $r \operatorname{cis}(2\theta)$
(e) r (f) $2r \cos \theta$
(g) $(1/r) \operatorname{cis}(-\theta)$ (h) $(1/r) \operatorname{cis}(\pi/2 - \theta)$
(i) $r \operatorname{cis}(\pi/2 - \theta)$ (j) $r \operatorname{cis}(2\theta - \pi)$
(k) $1/r$ (l) $2r \sin \theta \operatorname{cis}(\pi/2)$

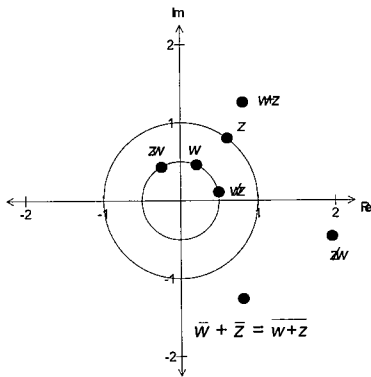
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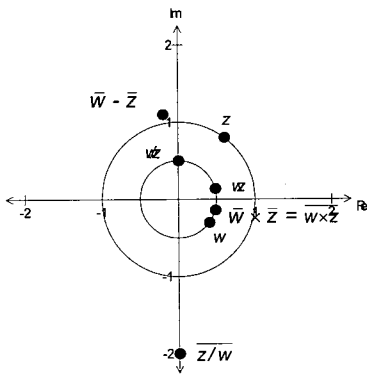
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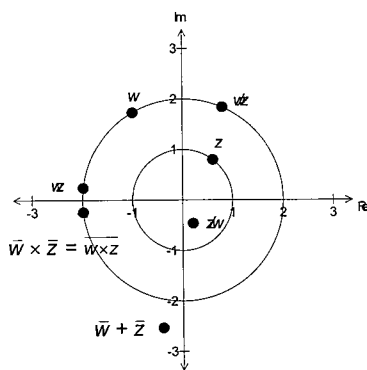
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8.

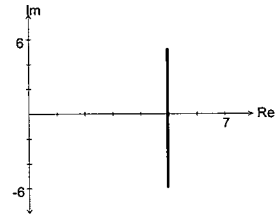


9.

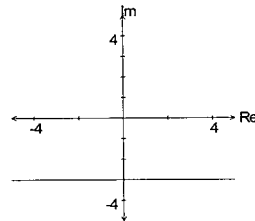


Exercise 1.4

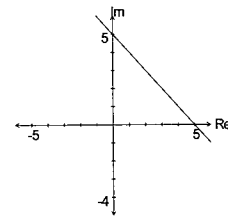
1. (a)



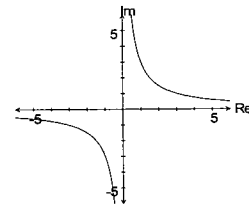
(b)



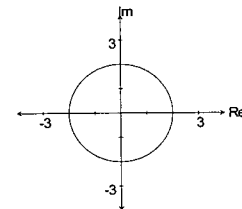
(c)



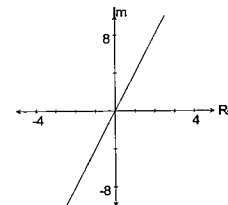
(d)



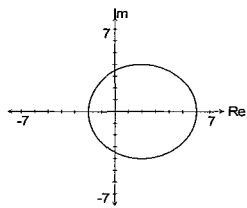
(e)



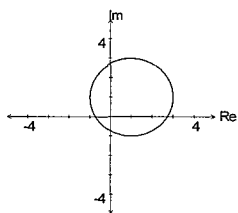
(f)



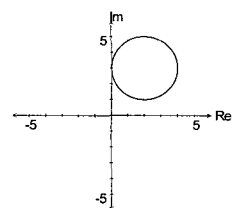
1. (g)



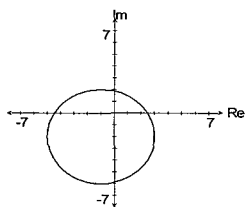
(h)



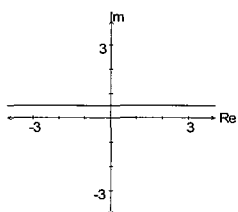
(i)



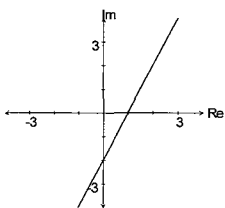
(j)



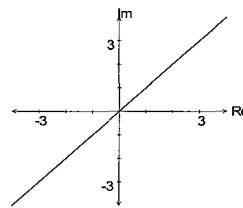
(k)



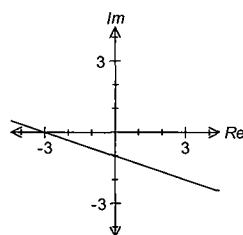
(l)



1. (m)

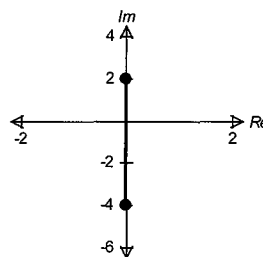


(n)

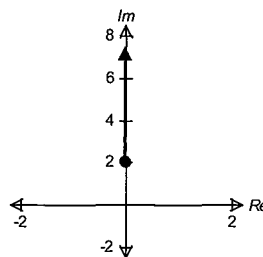


2. (a) $x = 5$ (b) $y = -3$ (c) $x + y = 5$
 (d) $xy = 3$ (e) $x^2 + y^2 = 4$ (f) $y = 4x$
 (g) $(x - 2)^2 + y^2 = 16$
 (h) $(x - 1)^2 + (y - 1)^2 = 4$
 (i) $(x - 2)^2 + (y - 3)^2 = 4$
 (j) $(x + 1)^2 + (y + 2)^2 = 16$
 (k) $y = 1/2$ (l) $y = x - 2$
 (m) $y = x$ (n) $y = (-x/3) - 1$

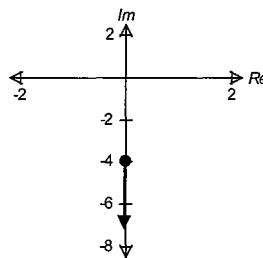
3. (a)



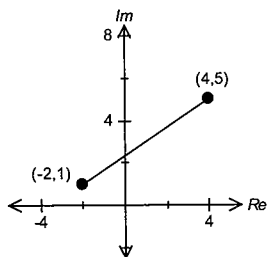
(b)



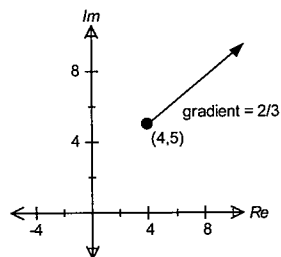
(c)



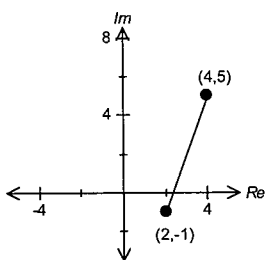
4. (a)



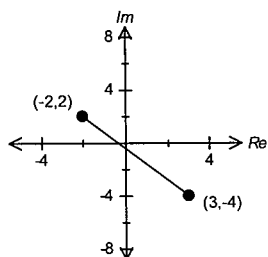
(b)



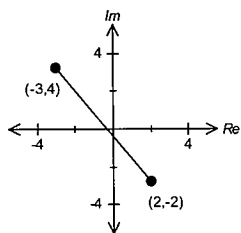
(c)



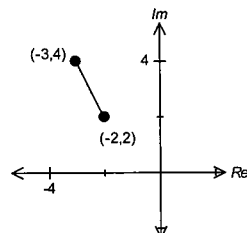
5. (a)



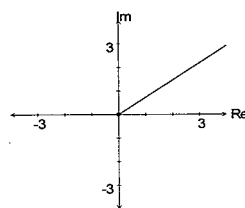
(b)



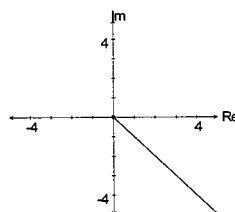
(c)



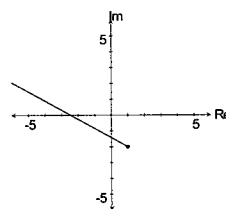
6. (a)



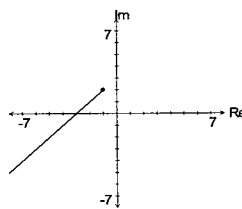
(b)



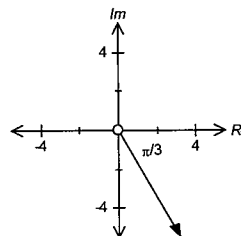
(c)



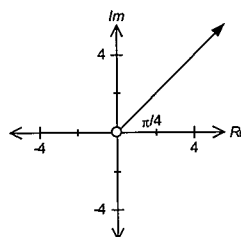
(d)



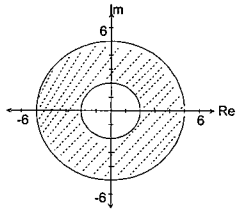
(e)



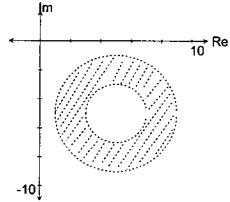
(f)



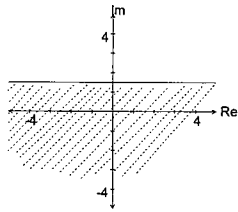
7. (a)



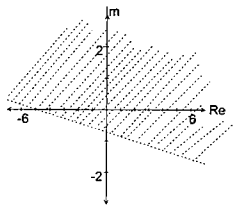
(b)



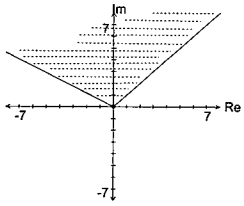
(c)



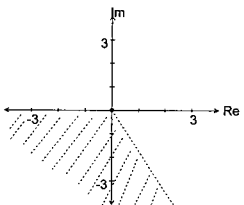
(d)



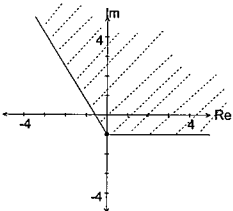
(e)



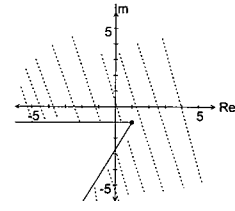
(f)



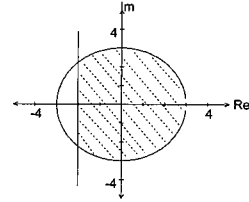
(g)



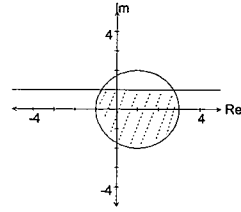
7. (h)



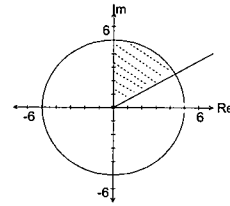
8. (a)



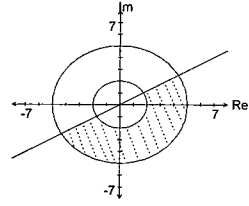
(b)



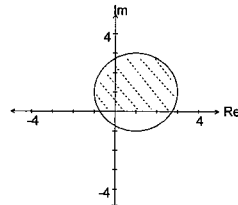
(c)



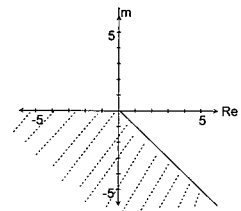
(d)



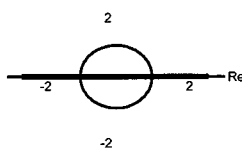
(e)



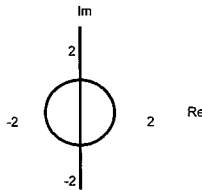
(f)



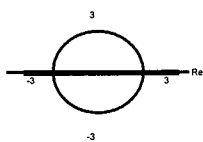
9. (a) $x^2 + y^2 = 1$ or $y = 0$



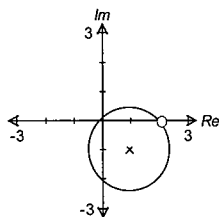
(b) $x^2 + y^2 = 1$ or $x = 0$



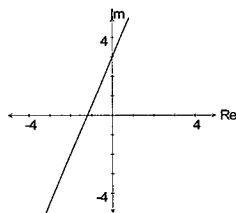
(c) $x^2 + y^2 = 4$ or $y = 0$



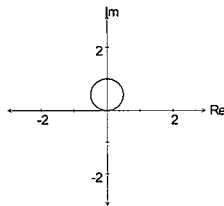
(d) $(x - 1)^2 + (y + 1)^2 = 2$ except the point (2,0)



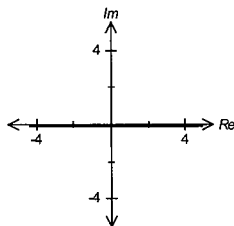
(e) $5x - 2y + 6 = 0$



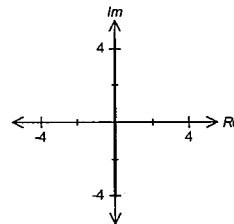
(f) $x^2 + (y - 1/2)^2 = 1/4$



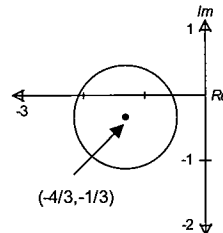
(g) $y = 0$



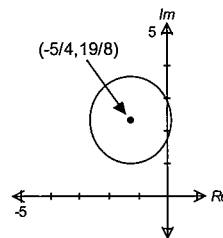
9. (h) $x = 0$



(i) $(x + 4/3)^2 + (y + 1/3)^2 = (2\sqrt{2}/3)^2$



(j) $(x + 5/4)^2 + (y - 19/8)^2 = 117/64$



10. (a) $\min \sqrt{2} - 1, \max \sqrt{2} + 1$

(b) $\min -\pi/2 \text{ rad}, \max 0 \text{ rad}$

11. (a) $0 < |z| \leq 10$

(b) $-0.64 < \arg(z) \leq 2.50 \text{ rad}$

12. (a) $0 < |z| \leq \sqrt{2}$

(b) $0 < \arg(z) \leq \pi/4$

13. (a) $\min 1, \max 2 + \sqrt{2}$

(b) $\min -1.25 \text{ rad}, \max \pi/4 \text{ rad}$

14. (a) $|z - 5| = |z - 5i|$

(b) $|z - (1 + i)| \leq 1$

(c) $-\pi/4 \leq \arg(z) \leq \pi/4$

(d) $|z - 2| \leq 3$ and $|z - 6| \leq 3$

(e) $|z - (-3 + 2i)| + |z - (7 + 2i)| = |(7 + 2i) - (-3 + 2i)|$

(f) $|z - (2 + 2i)| \leq 8$ and $\pi/4 \leq \arg(z) \leq \pi/2$

Exercise 2.1

1. (a) $\text{cis}(\pi/3), \text{cis}(\pi), \text{cis}(-\pi/3)$

(b) $2 \text{cis}(\pi/3), 2 \text{cis}(\pi), 2 \text{cis}(-\pi/3)$

(c) $\sqrt{2} \text{cis}(\pi/4), \sqrt{2} \text{cis}(3\pi/4), \sqrt{2} \text{cis}(-3\pi/4), \sqrt{2} \text{cis}(-\pi/4)$

(d) $\text{cis}(0), \text{cis}(2\pi/5), \text{cis}(4\pi/5), \text{cis}(-4\pi/5), \text{cis}(-2\pi/5)$

(e) $2 \text{cis}(0), 2 \text{cis}(2\pi/5), 2 \text{cis}(4\pi/5), 2 \text{cis}(-4\pi/5), 2 \text{cis}(-2\pi/5)$

(f) $2 \text{cis}(0), 2 \text{cis}(\pi/3), 2 \text{cis}(2\pi/3), 2 \text{cis}(\pi), 2 \text{cis}(-2\pi/3), 2 \text{cis}(-\pi/3)$

2. (a) $0.9239 + 0.3827i, -0.9239 - 0.3827i, -0.3827 + 0.9239i, 0.3827 - 0.9239i$

(b) $\pm 0.9511 - 0.3090i, \pm 0.5878 + 0.8090i, -i$

(c) $1.0696 + 0.2127i, -1.0696 - 0.2127i, -0.2127 + 1.0696i, 0.2127 - 1.0696i$

2. (d) $1.1236 + 0.2388i, 0.1201 + 1.1424i,$
 $-1.0494 + 0.4672i, -0.7686 - 0.8536i$
 $0.5743 - 0.9948i$
 (e) $1.0548 - 0.3839i, 0.8599 + 0.7215i,$
 $-0.1949 + 1.1054i, -1.0548 + 0.3839i,$
 $-0.8599 - 0.7215i, 0.1949 - 1.1054i$
 (f) $-1.5, 0.75 \pm 1.2990i$
4. $\pm 1, (\pm 0.5 \pm 0.8660i)$
5. $w = (-1/2) + (\sqrt{3}/2)i, w^2 = (-1/2) - (\sqrt{3}/2)i,$
 $w^3 = 1; z = 1$
6. $3 \operatorname{cis}(\pi), 3 \operatorname{cis}(3\pi/5), 3 \operatorname{cis}(-3\pi/5), 3 \operatorname{cis}(\pi/5),$
 $3 \operatorname{cis}(-\pi/5); z^5 = -243$
7. $2 \operatorname{cis}(\pi/3), 2 \operatorname{cis}(2\pi/3), 2 \operatorname{cis}(\pi), 2 \operatorname{cis}(-2\pi/3),$
 $2 \operatorname{cis}(-\pi/3), 2 \operatorname{cis}(0); z^6 = 64$
8. $\sqrt{2} \operatorname{cis}(-\pi/4), \sqrt{2} \operatorname{cis}(0), \sqrt{2} \operatorname{cis}(\pi/4),$
 $\sqrt{2} \operatorname{cis}(\pi/2), \sqrt{2} \operatorname{cis}(3\pi/4), \sqrt{2} \operatorname{cis}(\pi),$
 $\sqrt{2} \operatorname{cis}(-\pi/2), \sqrt{2} \operatorname{cis}(-3\pi/4); z^8 = 16$
9. $n = 5; \operatorname{cis}(\pm\pi/5), \operatorname{cis}(\pm3\pi/5), \operatorname{cis}(\pi)$
10. (a) $-1/2 \pm (\sqrt{3}/2)i, 1$
 (b) $\pm i, \pm 2i, \pm 1$
 (c) $-1/2 \pm (\sqrt{3}/2)i, \pm(\sqrt{3})/2 - (1/2)i, i$
 (d) $\pm(\sqrt{3}/2) + (1/2)i, \pm\sqrt{3} - i, -i, 2i$

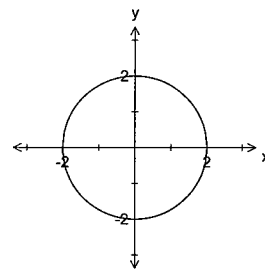
Exercise 2.2

3. $\sin(\pi/6)$ repeated, $\sin(3\pi/2)$
4. $\cos(\pi/9), \cos(5\pi/9), \cos(7\pi/9)$
5. $\cos(6\theta) = 32 \cos^2(\theta) - 48 \cos^4(\theta)$
 $+ 18 \cos^6(\theta) - 1$
 (a) $\cos(\pi/12), \cos(\pi/4), \cos(5\pi/12),$
 $\cos(7\pi/12), \cos(3\pi/4), \cos(11\pi/12)$
 (b) $\cos^2(\pi/12), \cos^2(\pi/4), \cos^2(5\pi/12)$
6. (a) $\cos(5\theta) = 16 \cos^5(\theta) - 20 \cos^3(\theta) + 5 \cos(\theta)$
 (b) $a = 16, b = -4, c = -4, d = 1$
 (c) $\cos(2\pi/5)$ repeated, $\cos(4\pi/5)$ repeated

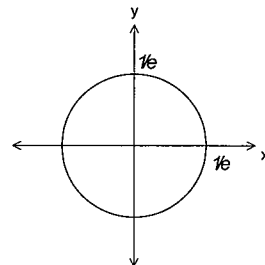
Exercise 2.3

1. (a) $2e^{i\pi}$ (b) $5e^{i3\pi/4}$
 (c) $3e^{-i\pi/6}$ (d) $\sqrt{2}e^{-i2\pi/3}$
2. (a) e^0 (b) $e^{i\pi/2}$ (c) $2e^{i\pi/3}$
 (d) $2\sqrt{2}e^{-i3\pi/4}$ (e) $2\sqrt{3}e^{-i\pi/6}$
3. (a) $\operatorname{cis}(\pi/6)$ (b) $\operatorname{cis}(-5\pi/6)$
 (c) $e \operatorname{cis}(-\pi/4)$ (d) $(1/e^2) \operatorname{cis}(\pi/3)$
4. (a) $(-1/2) + i(\sqrt{3})/2$
 (b) $(-\sqrt{2})/2 + i(\sqrt{2})/2$
 (c) $1/(2e) - i(\sqrt{3})/(2e)$
 (d) $(-e^2\sqrt{3})/2 + i(e^2)/2$
5. (a) $4e^{-i\pi/3}$ (b) $2\sqrt{2}e^{i7\pi/12}$
 (c) $\sqrt{2}e^{-i3\pi/4}$ (d) $2e^{i\pi/6}$

5. (e) 2 (f) $2e^{i\pi/2}$
 (g) $2\sqrt{2}e^{-i7\pi/12}$ (h) $2\sqrt{2}e^{-i7\pi/12}$
6. (a) $12e^{i2\pi/3}$ (b) $12e^{i2\pi/3}$
 (c) $\frac{\sqrt{2}}{4}e^{i\pi/4}$ (d) $\frac{\sqrt{2}}{4}e^{i\pi/4}$
 (e) $\sqrt{\frac{3}{2}}e^{i7\pi/12}$ (f) $\sqrt{\frac{3}{2}}e^{i7\pi/12}$
7. (a) $\frac{\sqrt{2}}{2} \operatorname{cis}(\frac{\pi}{6})$ (b) $2\sqrt{2} \operatorname{cis}(\frac{5\pi}{6})$
 (c) $\frac{\sqrt{2}}{2} \operatorname{cis}(-\frac{\pi}{6})$ (d) $\frac{\sqrt{2}}{2} \operatorname{cis}(-\frac{\pi}{6})$
 (e) $2\sqrt{2} \operatorname{cis}(-\frac{5\pi}{6})$ (f) $2\sqrt{2} \operatorname{cis}(\frac{5\pi}{6})$
12. (a) $x = 0, y = \pi$ (b) $x = \ln 2, y = \pi$
 (c) $x = \ln 2, y = 0$ (d) $x = 0, y = \pi/2$
 (e) $x = \ln \sqrt{2}, y = \pi/4$
13. (a) $a = 0, b = \pi$ (b) $a = \ln 2, b = \pi$
 (c) $a = \ln 3, b = \pi$
14. $a = \ln k^2, y = \pi$
15. $\operatorname{Max} \operatorname{Re}(z) = 2, \operatorname{Min} \operatorname{Im}(z) = -2$



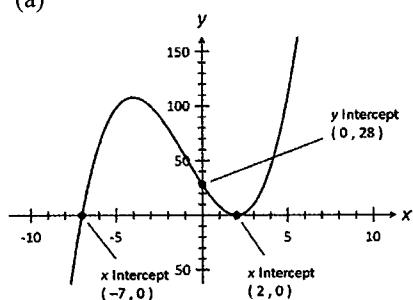
16. $\operatorname{Min} \operatorname{Re}(z) = -1/e, \operatorname{Max} \operatorname{Im}(z) = 1/e$



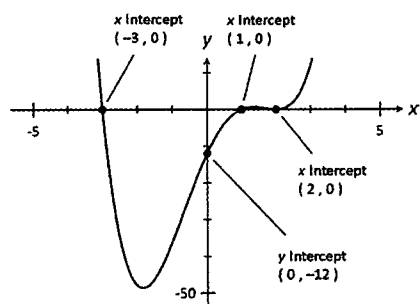
Exercise 3.1

1. $a = 6, b = -4$ 2. $k = -1$
 3. $a = 2, b = 0, c = 5$ 4. $a = -3, b = 0, c = 7$
 5. (a) $(x+1)(x+2)(x+3)(x+4)$
 (b) $(x+1)(x+2)$
 (c) $(x-1)(x-2)(x+3)$
 (d) $(x+1)(x-2)(2x-1)(2x+1)$
 (e) $(x-1)(2x+1)(x^2+1)$
 (f) $(x-1)(x-2)(x+4)$

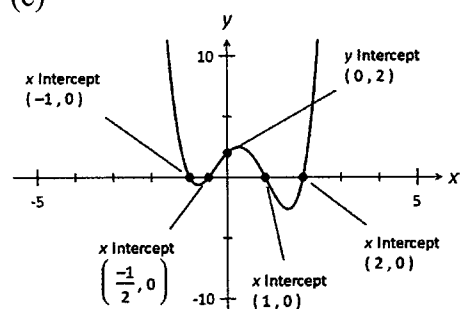
6. $(x^3 + 3)(x - 2)(x - 1)(x + 1)$
 7. (a)



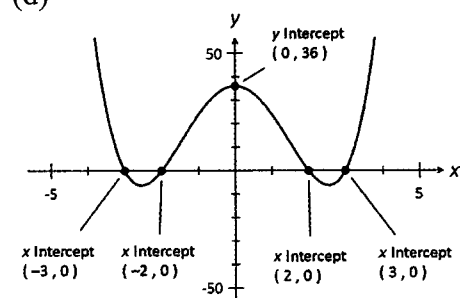
(b)



(c)



(d)



8. (a) $-1, -2$ (b) $-1, 1$
 (c) $-1, 0, 1, 1/3, 2$ (d) $-1, -1/3, 1/2, 0, 1$
 (e) $\pm 2, 1 \pm \sqrt{2}$ (f) $-1, 2$
 9. $-1, 2/3, 1/2$
 (a) $-1/2, 1/3, 1/4$ (b) $\pm \sqrt{2/3}, \pm \sqrt{1/2}$
 (c) $-2/3, -1/2, 1$ (d) $-1, 3/2, 2$
 10. $-3, -1/2, 2$
 (a) $-2, 1/2, 3$ (b) $\pm \sqrt{2}$
 (c) $-2, -1/3, 1/2$ (d) $-1/2, 1/3, 2$

Exercise 3.2

1. (a) $(x^2 - 2x + 8), -23$; $x, 8x - 7$
 (b) $3x^2/2 - 7x/4 - 39/8, 57/8$; $3x - 2, -16x + 16$

1. (c) $-2x^2 + 4x - 7/2, 17/2$; $-2x + 4, -9x + 9$
 (d) $6x^2 + 7x + 16x + 27, 64$
 $6x^2 - 5x + 26, -25x + 114$
 $3x - 4, 3x^2 + 5x + 2$
 2. $p = 1, q = 3$ 3. $p = 12/5, q = -24/5$
 4. $p = -5, q = 7$ 5. $p = 3, q = 5$
 6. $a = 1, b = -5$ 7. $a = -35, b = -23$
 8. $a = 1, b = -2$
 9. $p = 9, q = -2, r = -11$
 10. $p = -8, q = 3, r = 9$
 11. $a = 3, b = 4$
 12. $a = 6, b = -7$
 13. (b) $a = -3, b = -2$ (c) $5(2x + 3)$
 14. $a = 2, b = 1, c = 3$; 103

Exercise 3.3

1. (a) $(z - i)(z + i)(z + 2)$
 (b) $(z - 2i)(z + 2i)(z + 2)$
 (c) $(2z + i)(2z - i)(z - 1)$
 (d) $(z - (1 - i))(z - (1 + i))(z + 4)$
 2. $a = -4, b = 16$; $(z - 4i)(z + 4i)(z - 4)$
 3. $a = -2, b = 4$; $(z - 1 - i)(z - 1 + i)(z + 2)$
 4. $a = 6, b = -15$; $1 \pm 2i, \pm \sqrt{3}$
 5. $a = 16, b = 4$; $-2 \pm i, \pm i/2$
 6. $a = 9, b = 2$; $-1 \pm \sqrt{2}i, \pm i/3$
 7. (a) $\pm 1, \pm i\sqrt{2}$ (b) $-1, 2, -1 \pm i$
 (c) $-1, 3, 1 \pm i\sqrt{2}$ (d) $\pm 2i, 2 \pm i$
 8. (a) $1, \pm (\sqrt{2}/2) \pm i(\sqrt{2}/2)$
 (b) $\pm 1, \pm (\sqrt{2}/2) \pm i(\sqrt{2}/2)$
 (c) $\pm 1, \pm 1/2 \pm i(\sqrt{3})/2$
 (d) $\pm 1, \pm 1/2 \pm i(\sqrt{3})/2$
 9. $a = 6, b = 0, c = 1$ 10. $a = 4, b = 4, c = 4$

Exercise 4.1

1. (a) Not an onto function.
 (b) Not an onto function.
 (c) Not an onto function.
 (d) Is an onto function.
 2. (a) Many to one function.
 (b) Many to one function.
 (c) One to one function.
 3. (a) One to one function.
 (b) Many to one function.
 (c) One to one function.
 (d) Many to one function.
 (e) One to one function.
 (f) Many to one function.
 (g) One to one function.
 (h) Many to one function.
 (i) Many to one function.
 (j) Many to one function.
 4. (a) $(-\infty, 3/2]$ or $[3/2, \infty)$
 (b) $(-\infty, -2]$ or $[-2, \infty)$
 (c) $(-\infty, -1)$ or $(-1, \infty)$
 (d) \mathbb{R}
 (e) $(-\infty, 2]$ or $[2, \infty)$
 (f) $(-\infty, 5/2]$ or $[5/2, \infty)$

4. (g) $[-7, -2]$ or $[-2, 3]$ (h) $[-2, 2]$ or $[2, 6]$
 (i) $[-2, 0]$ or $[0, 2]$ (j) $(-\infty, 0]$ or $[2, \infty)$
 5. (a) $[-\pi/4, \pi/4]$ (b) $[0, 2\pi]$
 (c) $[-3\pi/4, \pi/4]$ (d) $[0, \pi/2]$
 (e) $[-\pi, 0) \cup (0, \pi]$
 (f) $[-\pi/2 - \tan^{-1}(4/3), \pi/2 - \tan^{-1}(4/3)]$

Exercise 4.2

1. (a) Yes (b) No
 (c) Yes (d) No
 2. (a) Yes (b) Yes
 (c) Yes (d) Yes
 3. (a) Yes (b) No
 (c) Yes (d) No
 4. (a) Yes (b) No
 (c) Yes (d) No
 5. (a) x^2 (b) $(x-3)^2 + 3$
 (c) $x-6$ (d) $(x+3)^2 + 3$
 6. (a) $1/x^2$ (b) $1/(x+1)^2 - 1$
 (c) $(x+1)/(x+2)$ (d) $(x-1)^2 - 1$
 7. (a) e^{1+2x} (b) $1+2e^x$
 (c) e^{e^x} (c) $3+4x$
 8. (a) $1+x$ (b) $1/(2-x)$
 (c) $(x-1)/x$ (d) $x/(2x+1)$
 9. (a) Domain for f : \mathbb{R} , Range for f : \mathbb{R}
 Domain for g : $\mathbb{R} - \{0\}$
 Range for g : $\mathbb{R} - \{0\}$
 (b) $\mathbb{R} - \{5\}$
 (c) $1/(5-x)$; $\mathbb{R} - \{5\}$, $\mathbb{R} - \{0\}$.
 10. (a) Domain for f : \mathbb{R} , Range for f : $[-5, \infty)$
 Domain for g : $[-1, \infty)$
 Range for g : $[0, \infty)$
 (b) $[-1, \infty)$
 (c) $x-4$; $[-1, \infty)$, $[-5, \infty)$
 11. $(1, \infty)$; x , $(1, \infty)$, $(1, \infty)$
 12. $(-\infty, 1] \cup [1, \infty)$; $1 + |x|$, $(-\infty, -1] \cup [1, \infty)$,
 $[2, \infty)$
 13. (a) $\ln(1 + \sin x)$; Not a function.
 (b) $\sin(\ln x) + 1$; Is a function. \mathbb{R}^+ , $[0, 2]$
 14. (a) 5^{25-x} ; Is a function. $(-\infty, 25]$, \mathbb{R}^+
 (b) $25 - 5^x$; Not a function.
 15. $g(x) = x + 5$ 16. $g(x) = 1/(x-2)$
 17. $g(x) = -1/[2(x+1)]$ 18. $f(x) = 5 - x$
 19. $f(x) = 2x - 3$ 20. $g(x) = (x-3)^2 + 1$
 21. $g(x) = (x-1)/(3x-1)$

Exercise 4.3

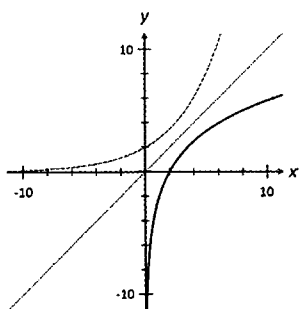
1. (a) Yes; domain \mathbb{R}^+ , range \mathbb{R}
 (b) No, $[-1, \infty)$ or $(-\infty, -1]$;
 domain \mathbb{R}_0^+ , range $[-1, \infty)$ or $(-\infty, -1]$

1. (c) No, $[-1, \infty)$ or $(-\infty, -1]$;
 domain $(-\infty, 1]$, range $[-1, \infty)$ or $(-\infty, -1]$
 (d) Yes; domain $[0, \infty)$ range $[1, \infty)$
 2. (a) Yes (b) No
 (c) No (d) Yes
 (e) Yes (f) Yes
 (g) Yes (h) Yes
 (i) No (j) No
 3. (a) $(x-3)/2$ (b) $-(4+x)/5$
 (c) $4 \pm \sqrt{x}$ (d) $2 \pm \sqrt[1/3]{1-x}$
 (e) $(-5 \pm \sqrt{x})/2$ (f) x^x
 (g) $[\ln(x) - 1]/2$ (h) $(e^x - 1)/2$
 (i) $(x-1)/x$ (j) $(1-x)/(x+1)$
 (k) $x^2 - 1$ (l) $(1+x)^2/x$
 4. (a) $x \geq -4$ or $x \leq -4$;
 $f^{-1}(x) = -4 + \sqrt{x}$, domain $x \geq 0$,
 range $y \geq -4$;
 $f^{-1}(x) = -4 - \sqrt{x}$, domain $x \geq 0$,
 range $y \leq -4$
 (b) $x \geq 2$ or $x \leq 2$;
 $f^{-1}(x) = 2 + \sqrt{x-1}$, domain $x \geq 1$,
 range $y \geq 2$
 $f^{-1}(x) = 2 - \sqrt{x-1}$, domain $x \geq 1$,
 range $y \leq 2$
 (c) $x \geq 0$ or $x \leq 0$;
 $f^{-1}(x) = \sqrt{x+1}$, domain $x \geq -1$,
 range $y \geq 0$
 $f^{-1}(x) = -\sqrt{x+1}$, domain $x \geq -1$,
 range $y \leq 0$
 (d) $x \geq -1$ or $x \leq -1$;
 $f^{-1}(x) = -1 + \sqrt{x-1}$, domain $x \geq 1$,
 range $y \geq -1$
 $f^{-1}(x) = -1 - \sqrt{x-1}$, domain $x \geq 1$,
 range $y \leq -1$
 (e) $x \geq 0$ or $x \leq 0$;
 $f^{-1}(x) = \sqrt{[(1/x) - 1]}$, domain $0 < x \leq 1$,
 range $y \geq 0$
 $f^{-1}(x) = -1\sqrt{[(1/x) - 1]}$, domain $0 < x \leq 1$,
 range $y \leq 0$
 (f) $x > 1$ or $x < 1$;
 $f^{-1}(x) = 1 + \sqrt{1/x}$, domain $x > 0$,
 range $y > 1$
 $f^{-1}(x) = 1 - \sqrt{1/x}$, domain $x > 0$,
 range $y < 1$
 (g) $-\pi/2 \leq x \leq \pi/2$;
 $f^{-1}(x) = \sin^{-1} x$, domain $-1 \leq x \leq 1$,
 range $-\pi/2 \leq y \leq \pi/2$
 (h) $0 \leq x \leq \pi/2$;
 $f^{-1}(x) = (\cos^{-1} x)/2$, domain $-1 \leq x \leq 1$,
 range $0 \leq y \leq \pi/2$

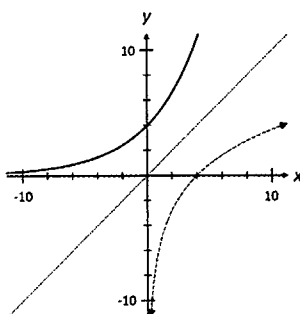
4. (i) $-\pi < x < \pi$;
 $f^{-1}(x) = \tan^{-1} x$, domain \mathbb{R} ,
 range $-\pi < y < \pi$
5. (a) $\sqrt{1 - e^x}$; $(-\infty, 0]$, $[0, 1]$
 (b) $e^{\sqrt{1-x}}$; $(-\infty, 1]$, $[1, \infty)$
 (c) $\ln(1-x)$; $1 - (\ln x)^2$
6. (a) $(x-1)/2$; $4 - 1/x$; $(3 - 1/x)/2$
7. (a) $x^2 - 1$; $1/x - 1$; $1/(x^2 - 1) - 1$
8. (a) Domain of f : \mathbb{R}_0^+ . Domain of g : \mathbb{R}_0^+ .
 (b) Domain of f : \mathbb{R}_0^+ . Domain of g : \mathbb{R}_0^+ .
9. (a) Domain of f : $(-\infty, 1]$.
 Domain of g : \mathbb{R}_0^+ .
 (b) Domain of f : $(-\infty, 1]$.
 Domain of g : \mathbb{R}_0^+ .
10. Domain of f : $(-1, \infty)$. Domain of g : $(0, \infty)$.

Exercise 5.1

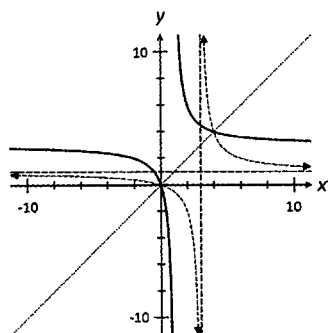
1. (a)



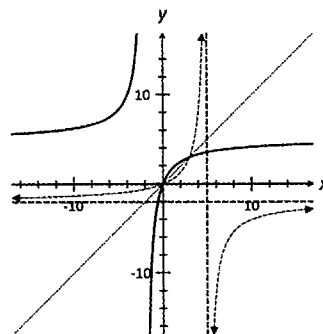
(b)



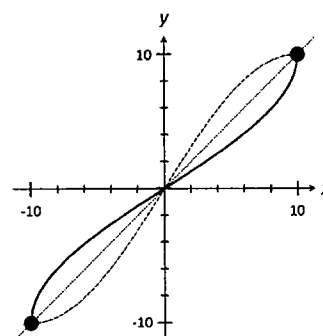
(c)



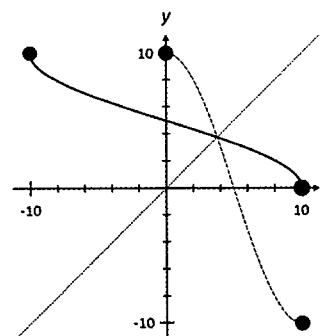
1. (d)



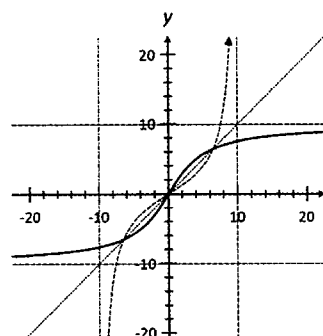
2. (a)



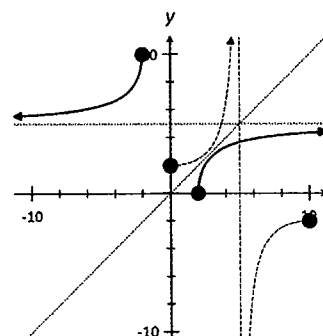
(b)



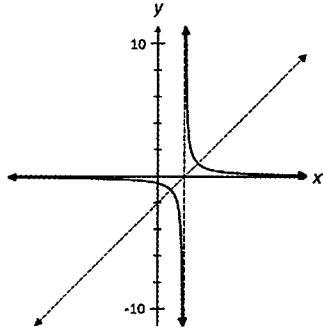
(c)



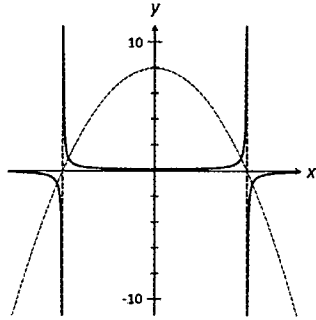
(d)



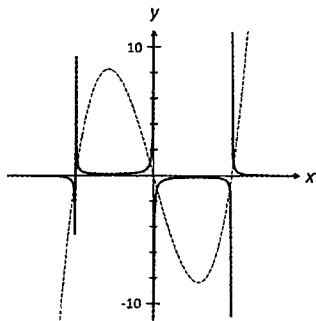
3. (a)



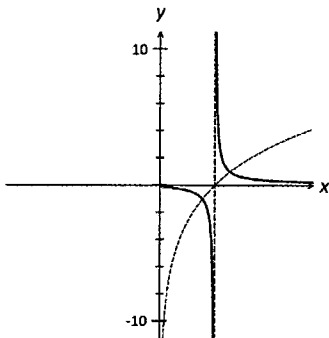
(b)



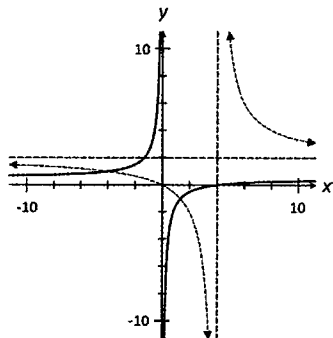
(c)



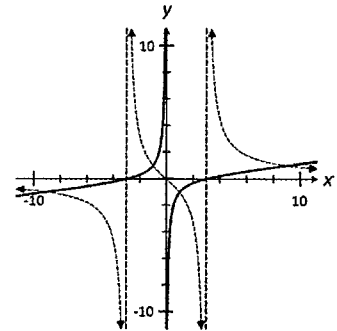
(d)



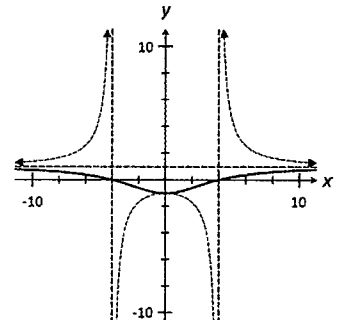
4. (a)



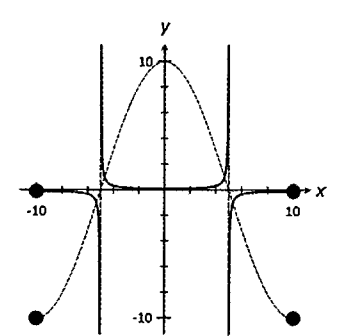
4. (b)



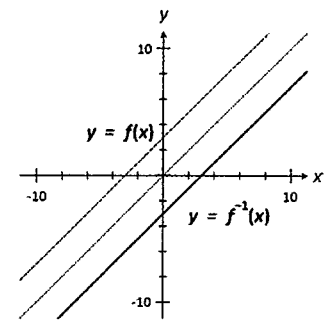
(c)



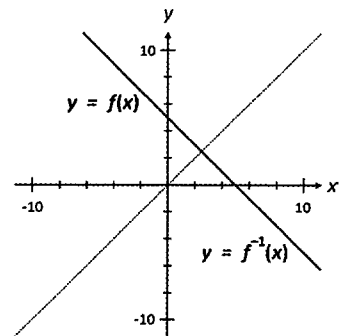
(d)



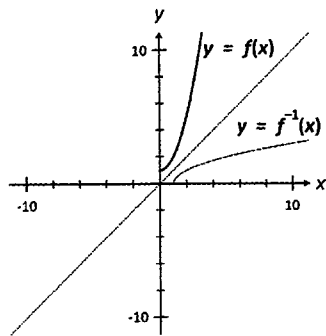
5. (a)



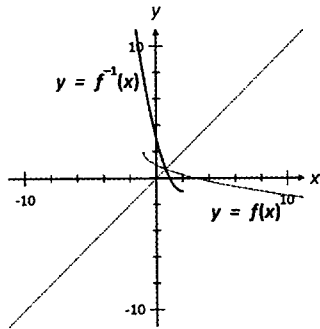
(b)



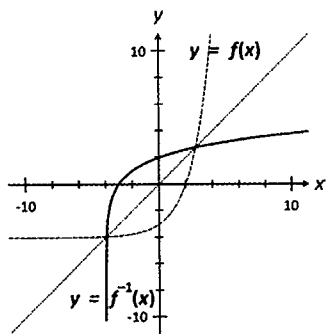
5. (c)



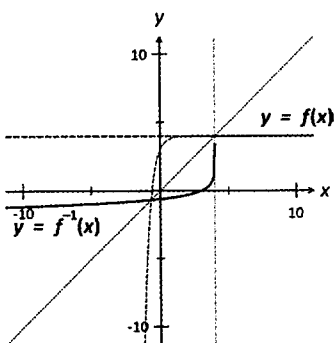
(d)



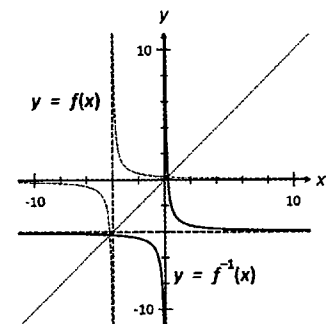
(e)



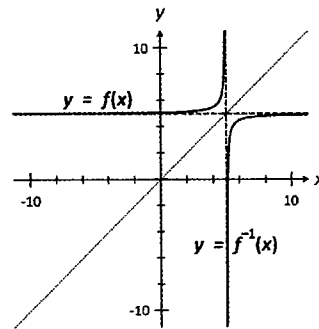
(f)



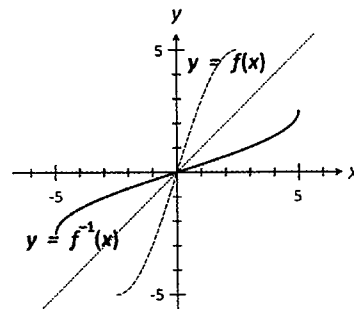
(g)



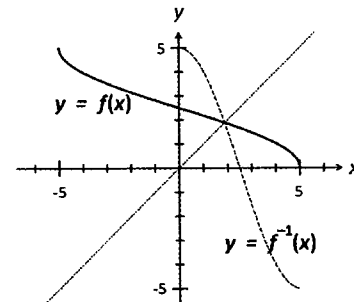
5. (h)



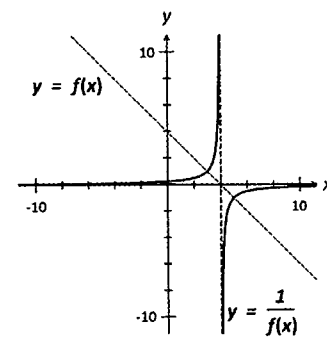
(i)



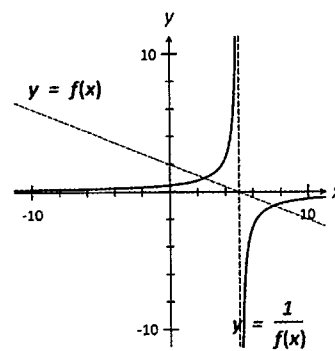
(j)



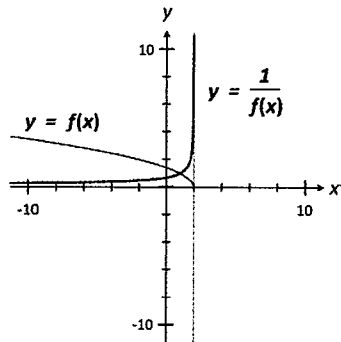
6. (a)



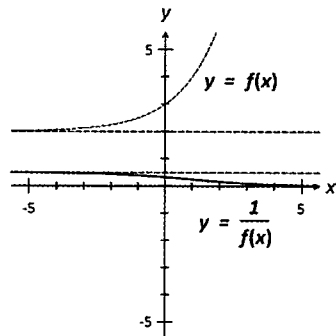
(b)



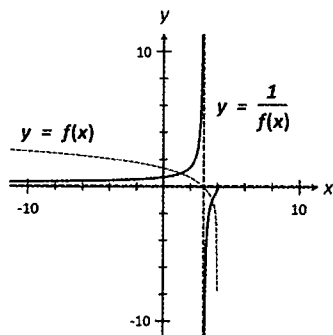
6. (c)



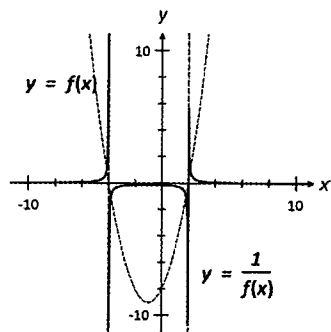
(d)



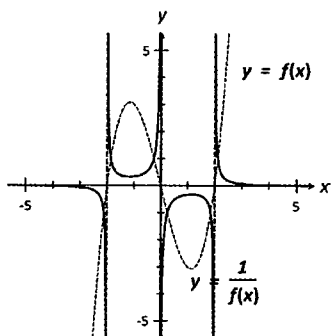
(e)



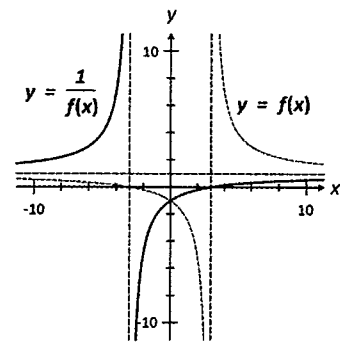
(f)



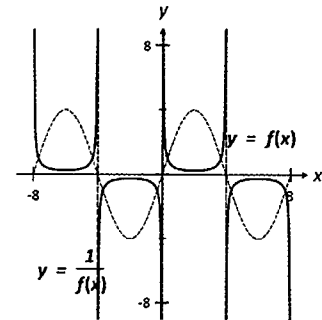
(g)



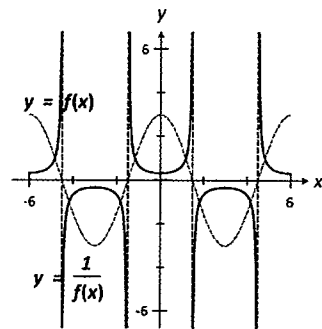
6. (h)



(i)

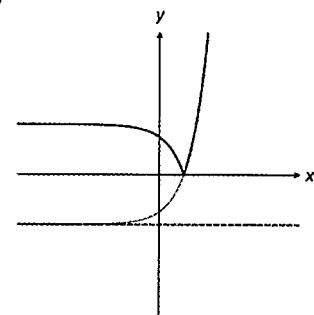


(j)

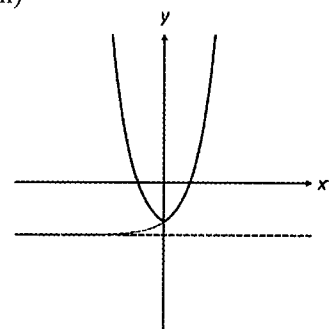


Exercise 5.2

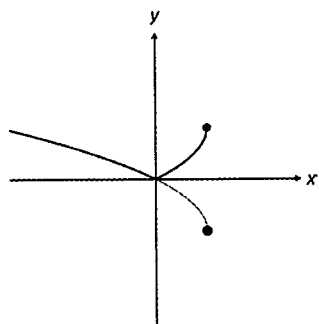
1. (a) (i)



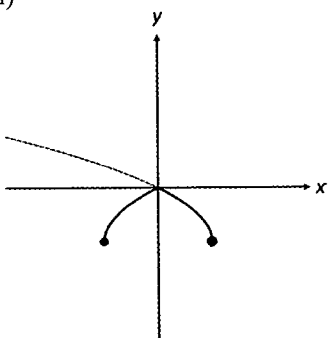
(ii)



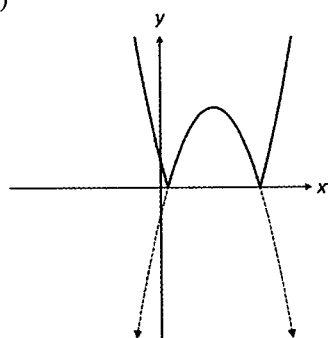
1. (b) (i)



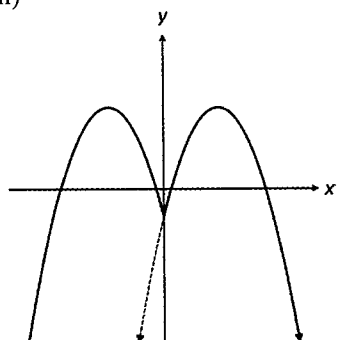
(ii)



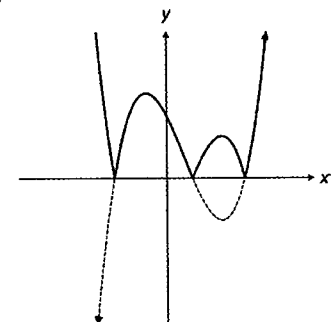
(c) (i)



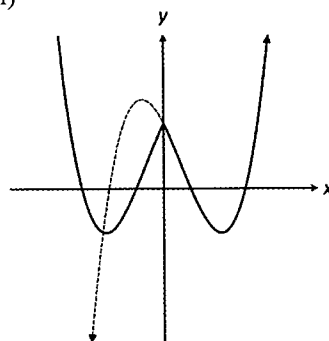
(ii)



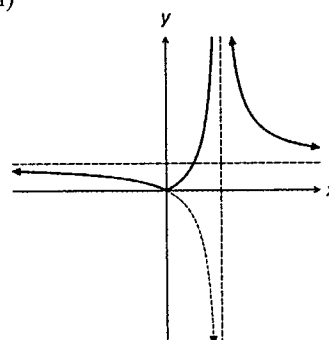
(d) (i)



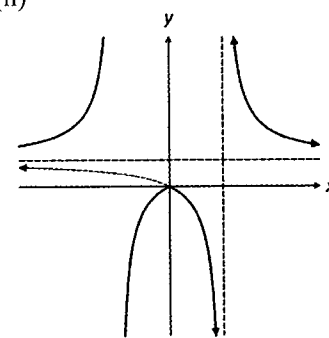
1. (d) (ii)



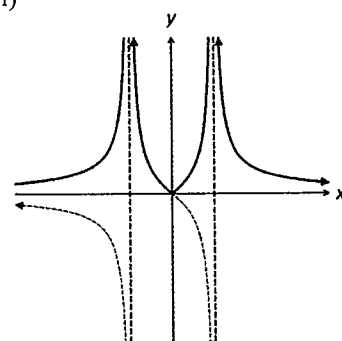
(e) (i)



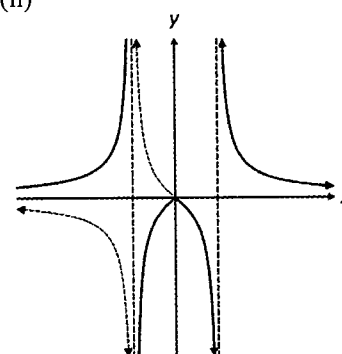
(ii)



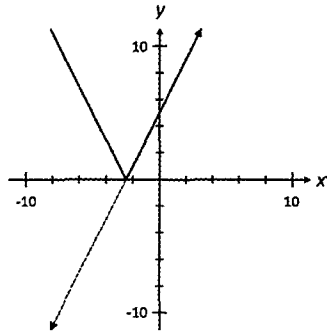
(f) (i)



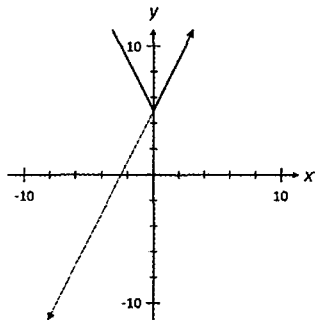
(ii)



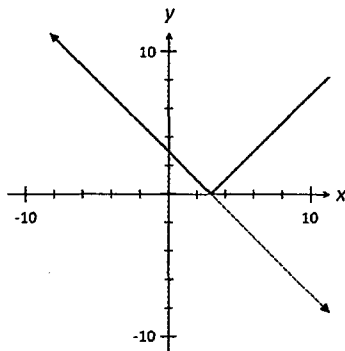
2. (a) (i) $|f(x)| = \begin{cases} -(2x+5) & x < -2.5 \\ 2x+5 & x \geq -2.5 \end{cases}$



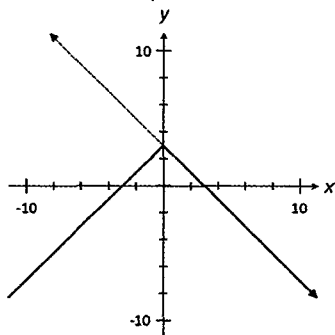
(ii) $f(|x|) = \begin{cases} -2x+5 & x < 0 \\ 2x+5 & x \geq 0 \end{cases}$



(b) (i) $|f(x)| = \begin{cases} 3-x & x < 3 \\ -(3-x) & x \geq 3 \end{cases}$

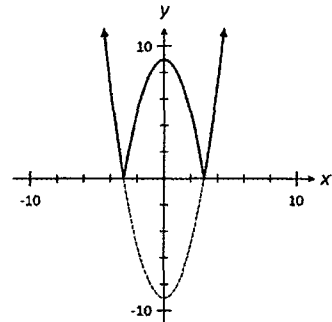


(ii) $f(|x|) = \begin{cases} 3+x & x < 0 \\ 3-x & x \geq 0 \end{cases}$

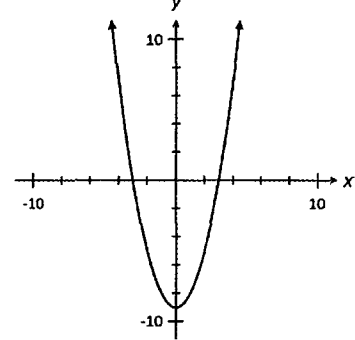


2. (c) (i)

$|f(x)| = \begin{cases} (x+3)(x-3) & x < -3, x > 3 \\ -(x+3)(x-3) & -3 \leq x \leq 3 \end{cases}$

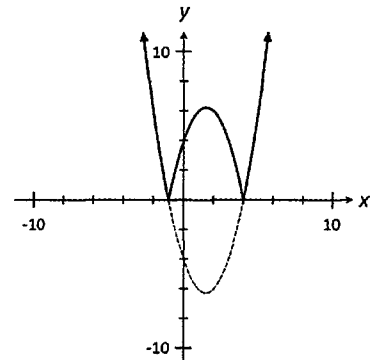


(ii) $f(|x|) = (x+3)(x-3)$

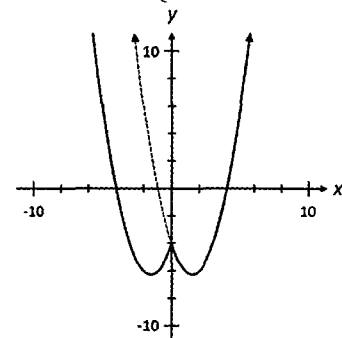


(d) (i)

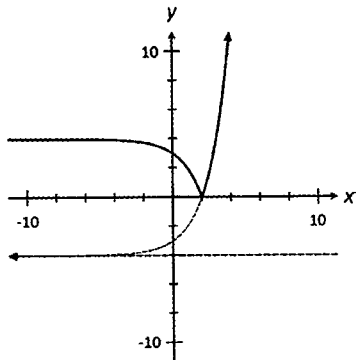
$|f(x)| = \begin{cases} x^2 - 3x - 4 & x < -1, x > 4 \\ -x^2 + 3x + 4 & -1 \leq x \leq 4 \end{cases}$



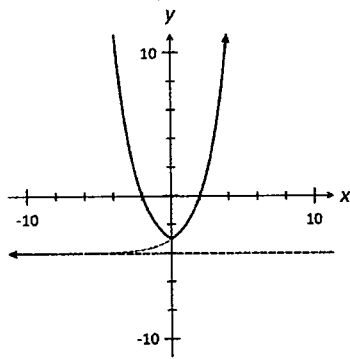
(ii) $f(|x|) = \begin{cases} x^2 + 3x - 4 & x < 0 \\ x^2 - 3x + 4 & x \geq 0 \end{cases}$



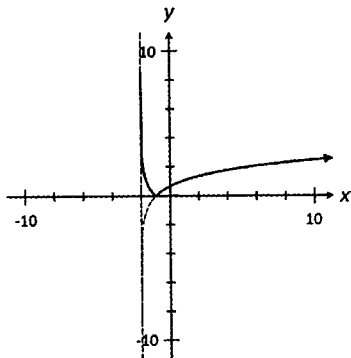
2. (e) (i) $|f(x)| = \begin{cases} 4-2^x & x < 2 \\ 2^x - 4 & x \geq 2 \end{cases}$



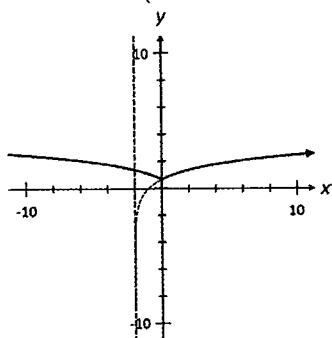
(ii) $f(|x|) = \begin{cases} 2^{-x} - 4 & x < 0 \\ 2^x - 4 & x \geq 0 \end{cases}$



(f) (i) $|f(x)| = \begin{cases} -\ln(x+2) & x < -1 \\ \ln(x+2) & x \geq -1 \end{cases}$

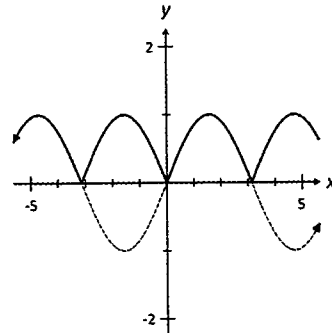


(ii) $f(|x|) = \begin{cases} \ln(-x+2) & x < 0 \\ \ln(x+2) & x \geq 0 \end{cases}$

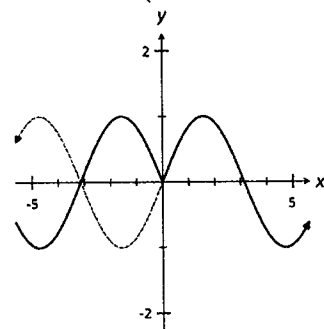


2. (g) (i)

$$|f(x)| = \begin{cases} -\sin x & (2n-1)\pi < x < 2n\pi \\ \sin x & 2n\pi \leq x \leq (2n+1)\pi \end{cases}$$

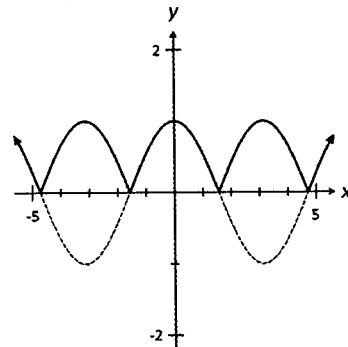


(ii) $f(|x|) = \begin{cases} \sin(-x) & x < 0 \\ \sin(x) & x \geq 0 \end{cases}$

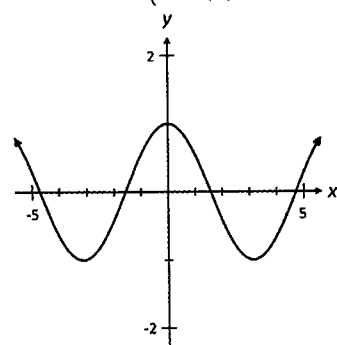


(h) (i) $|f(x)| =$

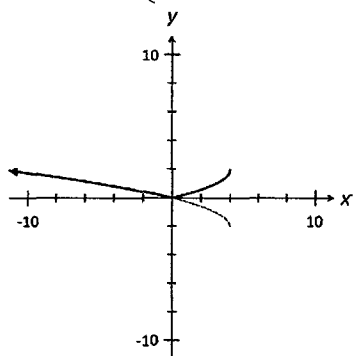
$$\begin{cases} -\cos x & \frac{(4n+1)\pi}{2} < x < \frac{(4n+3)\pi}{2} \\ \cos x & \frac{(4n-1)\pi}{2} \leq x \leq \frac{(4n+1)\pi}{2} \end{cases}$$



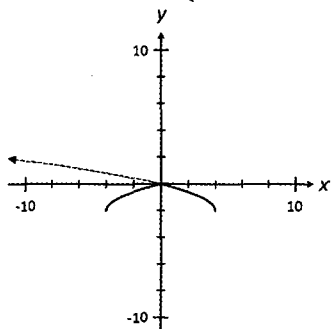
(ii) $f(|x|) = \begin{cases} \cos(-x) & x < 0 \\ \cos(x) & x \geq 0 \end{cases}$



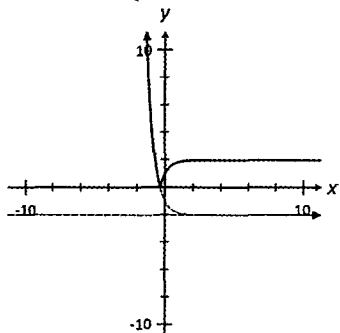
2. (i) (i) $|f(x)| = \begin{cases} \sqrt{4-x}-2 & x < 0 \\ 2-\sqrt{4-x} & x \geq 0 \end{cases}$



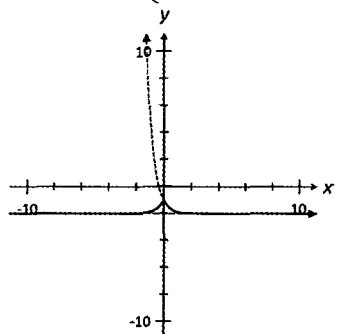
(ii) (i) $f(|x|) = \begin{cases} \sqrt{4+x}-2 & x < 0 \\ \sqrt{4-x}-2 & x \geq 0 \end{cases}$



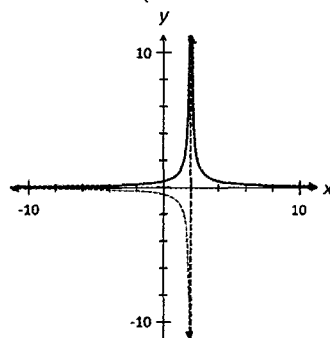
(j) (i) $|f(x)| = \begin{cases} e^{-2x}-2 & x < \frac{-\ln 2}{2} \\ 2-e^{-2x} & x \geq \frac{-\ln 2}{2} \end{cases}$



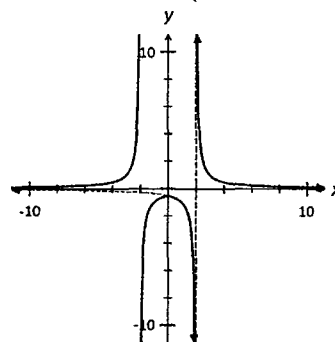
(ii) $f(|x|) = \begin{cases} e^{2x}-2 & x < 0 \\ e^{-2x}-2 & x \geq 0 \end{cases}$



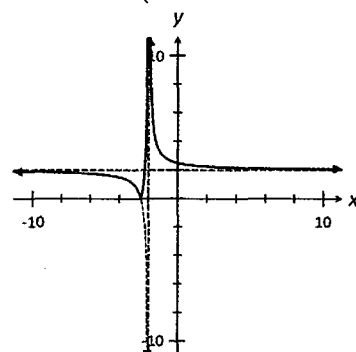
2. (k) (i) $|f(x)| = \begin{cases} -1/(x-2) & x < 2 \\ 1/(x-2) & x > 2 \end{cases}$



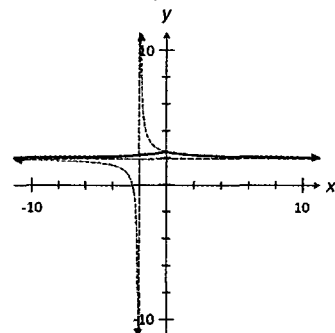
(ii) (i) $f(|x|) = \begin{cases} 1/(-x-2) & x < 2 \\ 1/(x-2) & x > 2 \end{cases}$



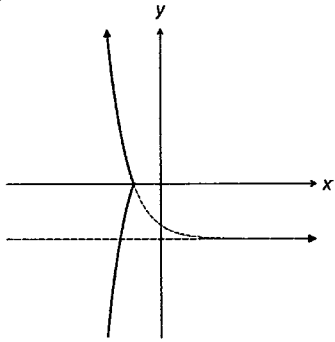
(j) (i) $|f(x)| = \begin{cases} -(1/(2+x)+2) & x < -5/2 \\ 1/(2+x)+2 & x > -5/2 \end{cases}$



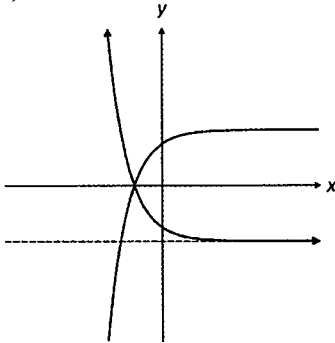
(ii) $f(|x|) = \begin{cases} 2+1/(2-x) & x < 0 \\ 2+1/(2+x) & x > 0 \end{cases}$



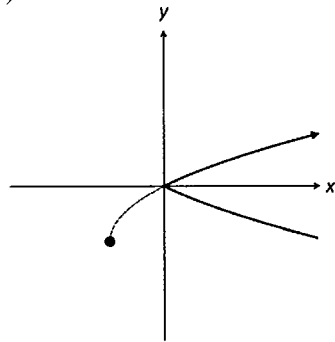
3. (a) (i)



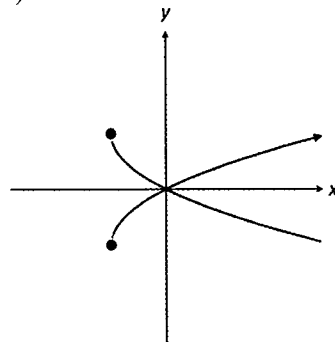
(ii)



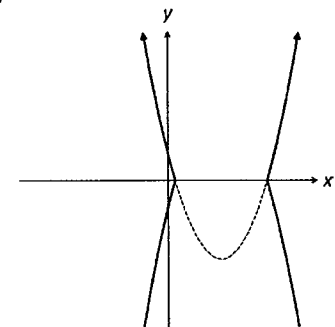
(b) (i)



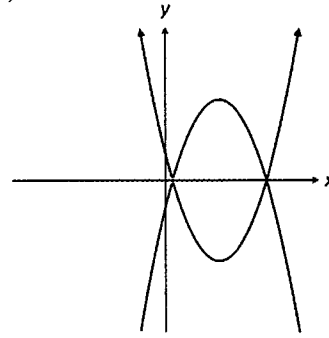
(ii)



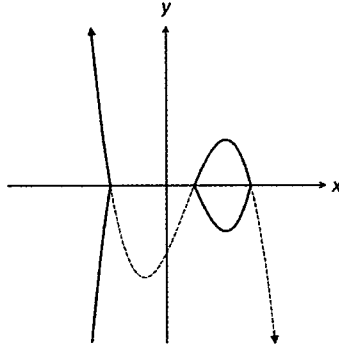
(c) (i)



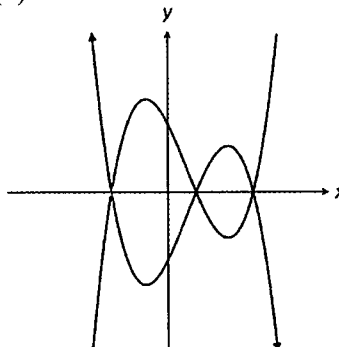
1. (c) (ii)



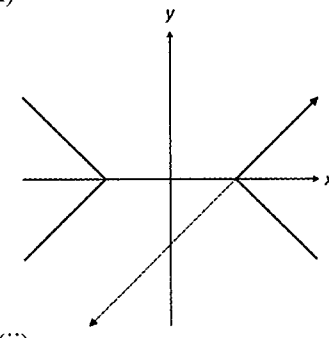
(d) (i)



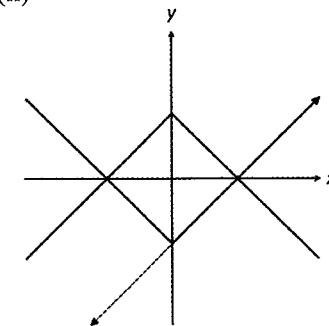
(ii)



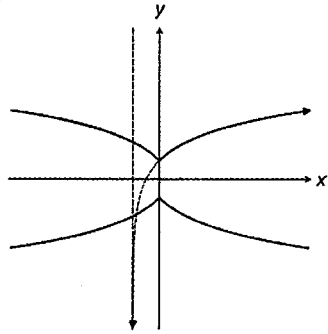
4. (a) (i)



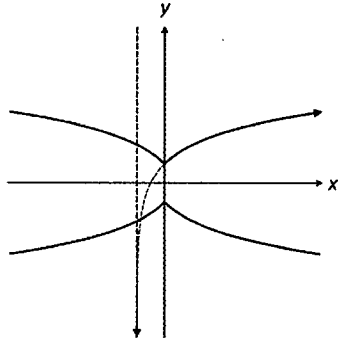
(ii)



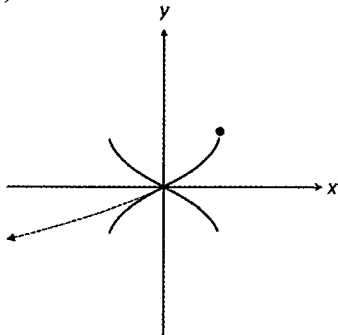
4. (b) (i)



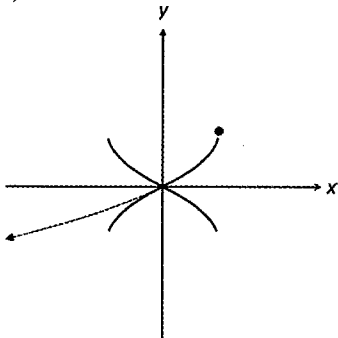
(ii)



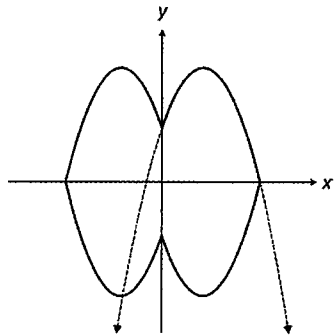
(c) (i)



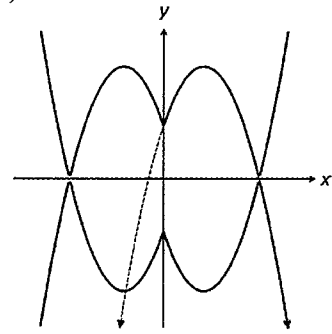
(ii)



(d) (i)

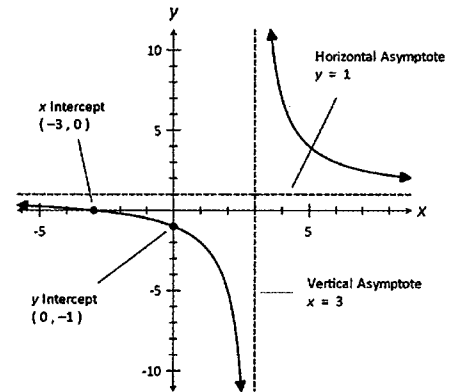


4. (d) (ii)

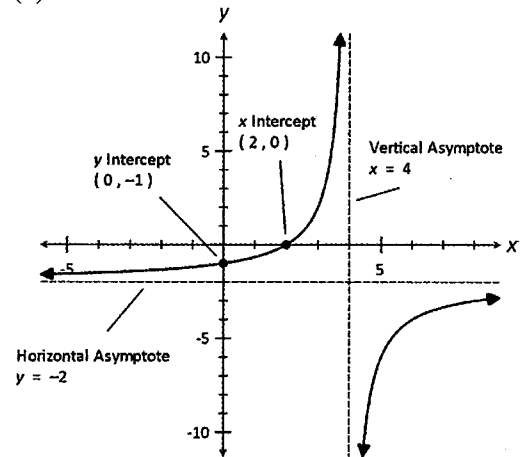


Exercise 5.3

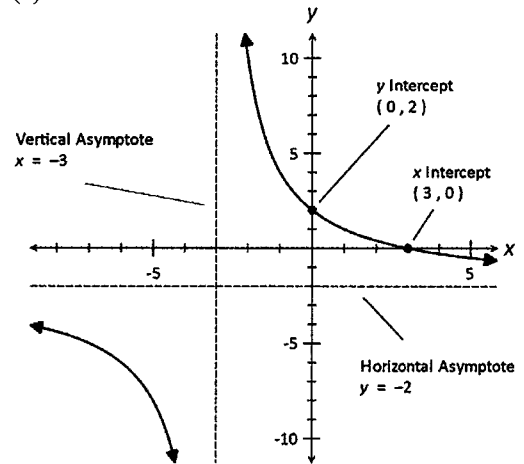
1. (a)



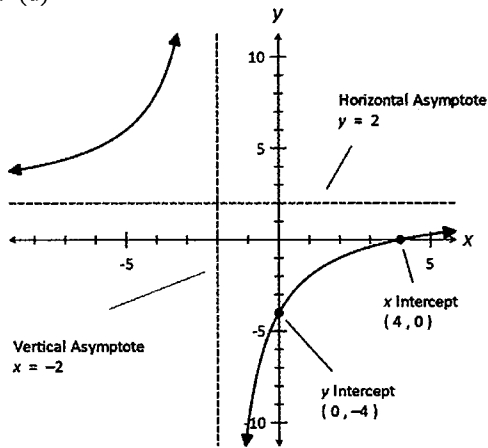
(b)



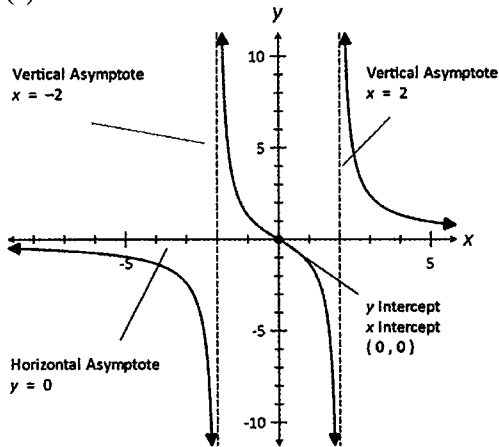
(c)



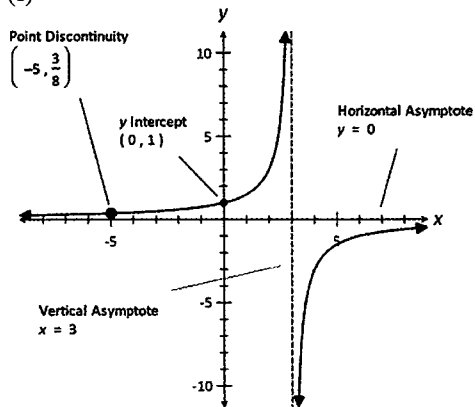
1. (d)



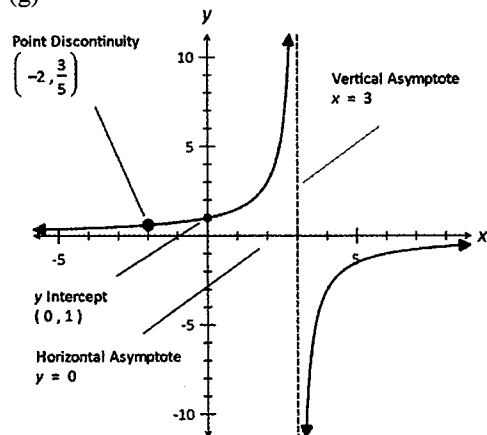
(e)



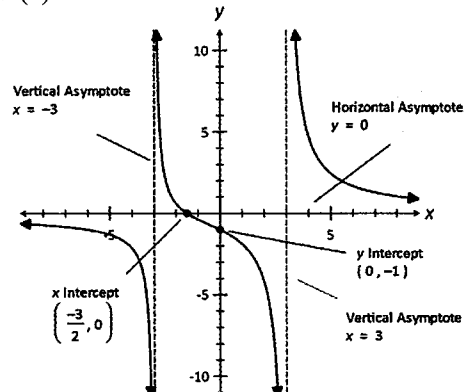
(f)



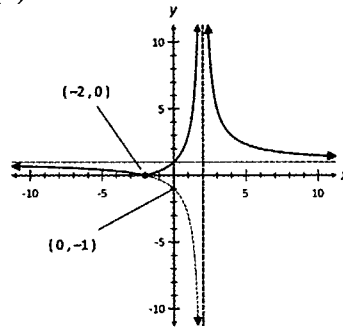
(g)



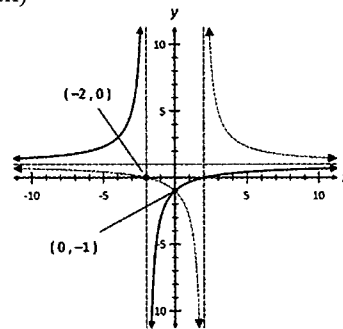
1. (h)



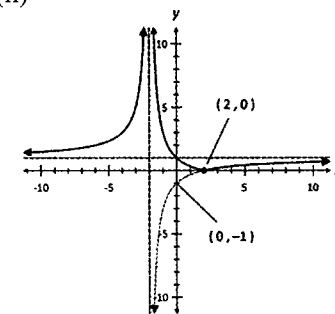
2. (a) (i) $y = (x + 2)/(x - 2)$
(ii)



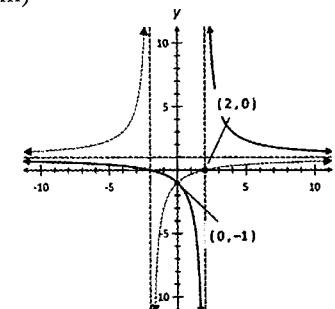
(iii)



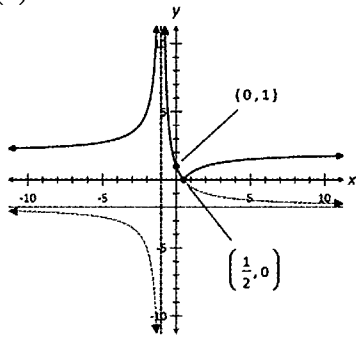
(b) (i) $y = (x - 2)/(x + 2)$
(ii)



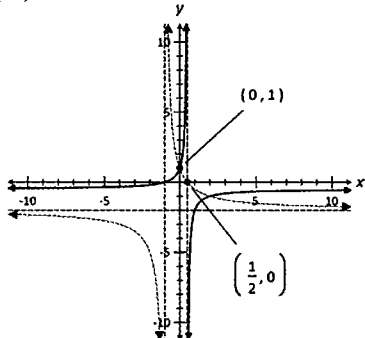
(iii)



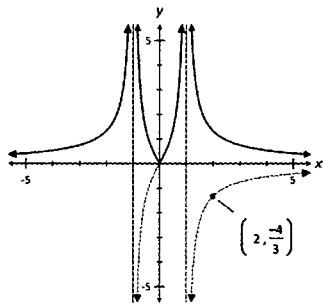
2. (c) (i) $y = (1 - 2x)/(x + 1)$
 (ii)



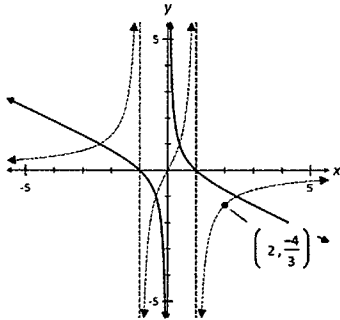
(iii)



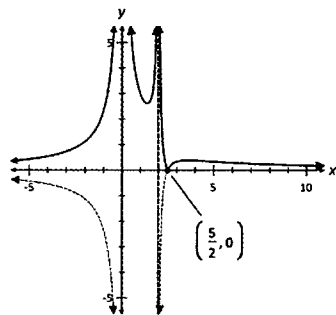
3. (a) $a = 2, b = 0, c = 1$
 (b)



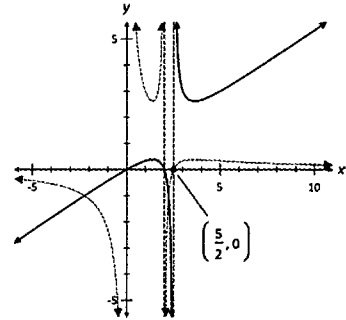
(c)



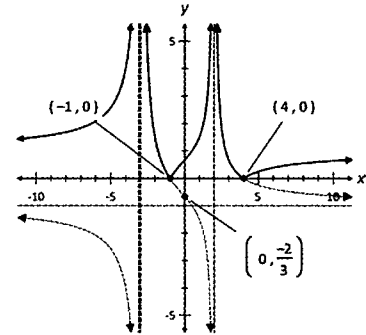
4. (a) $a = 2, b = -5, c = 1, d = 2$
 (b)



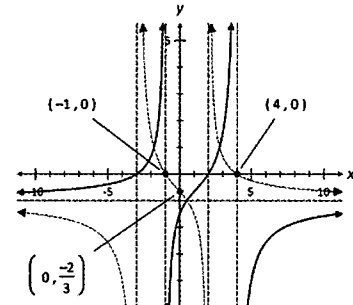
4. (c)



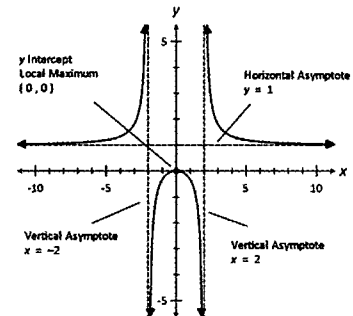
5. (a) $a = 4, b = 1, c = 3, d = -2$
 (b)



(c)

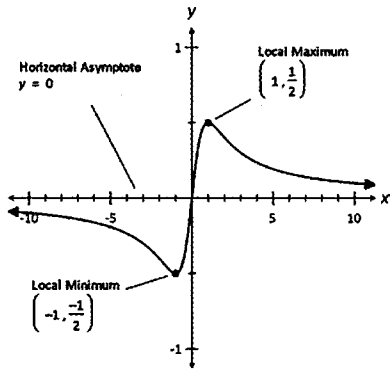


6. $a = k, b = -k, c = -2k, d = 4k, k$ is a real no.
 7. $a = 2, b = -1, c = 3, d = -1$
 8. $a = -1, b = 1, c = 1, d = -2$
 or $a = 1, b = -1, c = 1, d = -2$
 9. $a = 1, b = -1, c = 1, d = 2, e = 3, f = -3$
 ($ab = 1$ and $ad = -2$)
 10. (a) intercepts $(0, 0)$
 asymptotes $x = -2, x = 2, y = 1$
 (b) $a = -8$
 (c) max point $(0, 0)$
 (d)

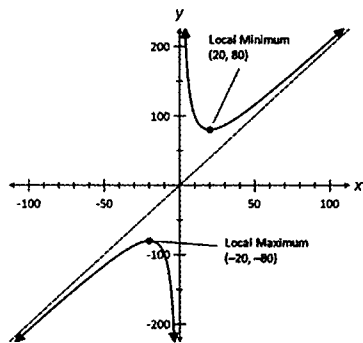


11. (a) intercepts $(0, 0)$; asymptotes $y = 0$
 (b) $a = 1, b = 1$

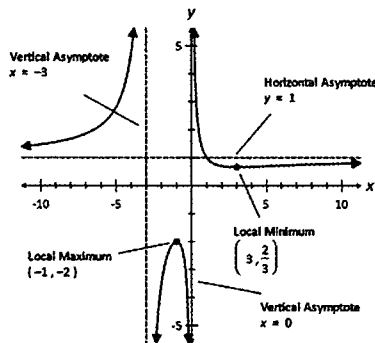
11. (c) min point $(-1, -1/2)$, max point $(1, 1/2)$
 (d)



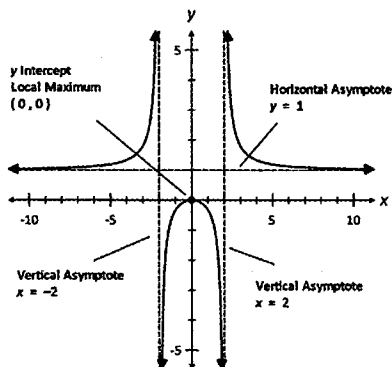
12. (a) no intercepts; asymptotes $x = 0$, oblique asymptote $y = 2x$
 (b) $a = 2, b = -800$
 (c) min point $(20, 80)$, max point $(-20, -80)$
 (d)



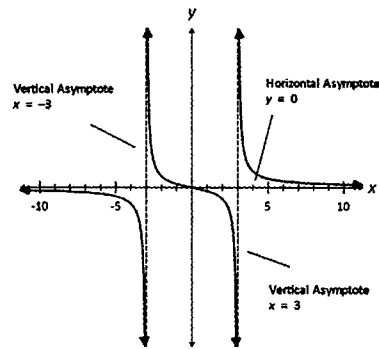
13. (a) no intercepts
 asymptotes $x = 0, x = -3, y = 1$
 (b) $a = 1, b = -3$ or $a = -3, b = 1$
 (c) min point $(3, 2/3)$, max point $(-1, -2)$
 (d)



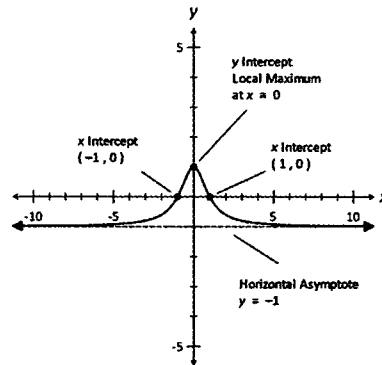
14.



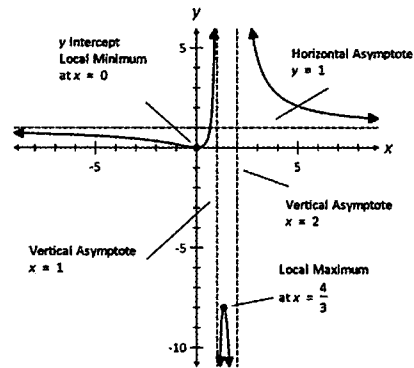
15.



16.

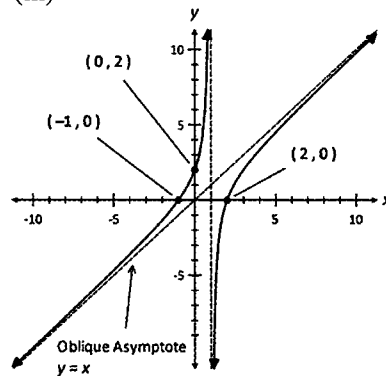


17.

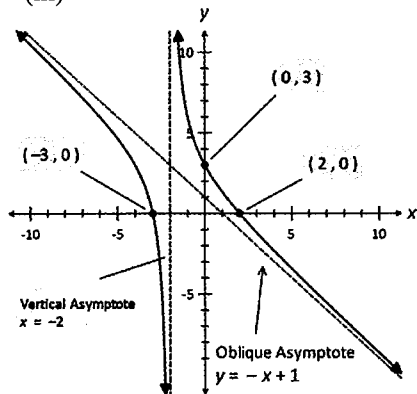


Exercise 5.4

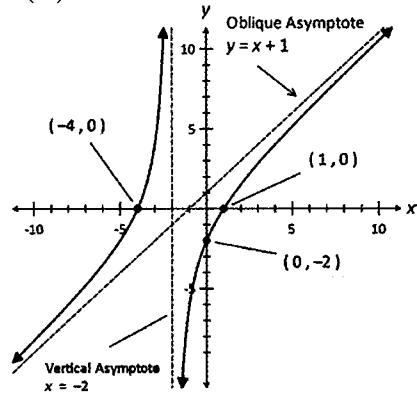
1. (a) (i) $y = x - 2/(x - 1)$
 (iii)



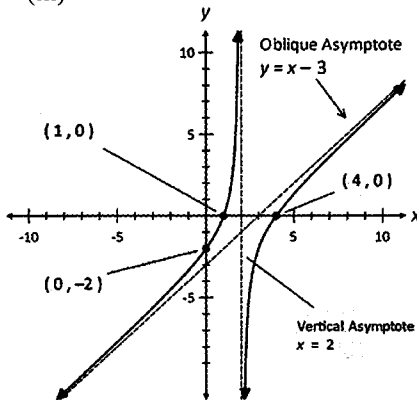
1. (b) (i) $y = -x + 1 + 4/(x + 2)$
(iii)



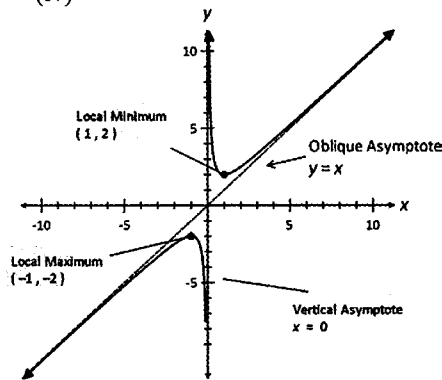
(c) (i) $y = x + 1 - 6/(x + 2)$
(iii)



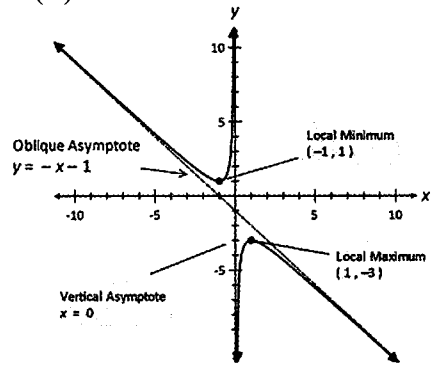
(d) (i) $y = x - 3 - 2/(x - 2)$
(iii)



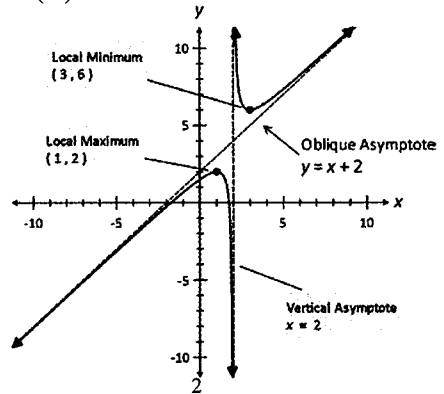
2. (a) (i) $y = x + 1/x$
(iv)



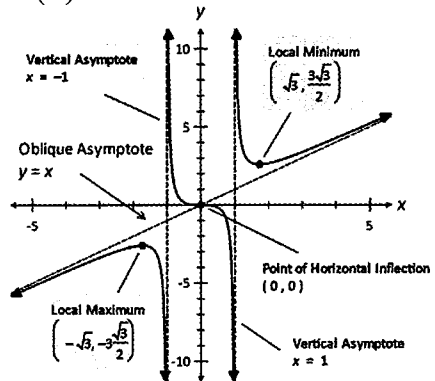
2. (b) (i) $y = -x - 1 - 1/x$
(iv)



(c) (i) $y = x + 2 + 1/(x - 2)$
(iv)



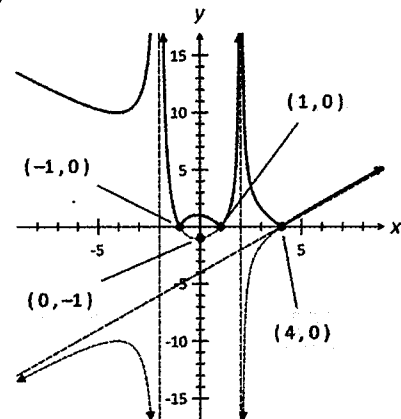
(d) (i) $y = x + x/(x - 1)$
(iv)



3. (a) $y = x - 4$

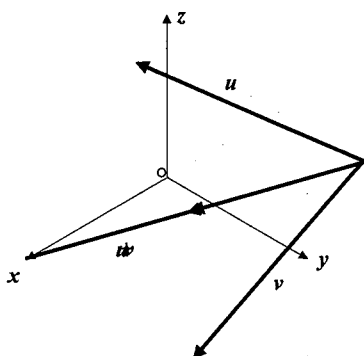
(b) $b = -4, c = -1, d = 4, n = -4$

(c)

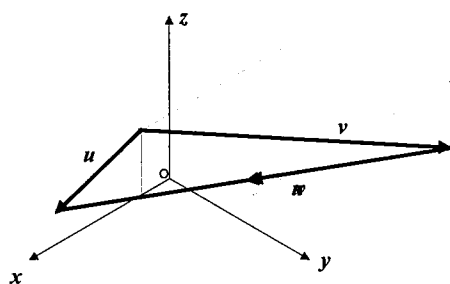


Exercise 6.1

1. (a)



(b)



2. (a) $\langle 10, 3, 2 \rangle$ (b) $\langle 4, -15/2, 11 \rangle$
 3. (a) $\pm 3\sqrt{43}$ (b) $10 \pm 10\sqrt{3}$
 4. $\langle 8, -8, 8 \rangle$
 5. (a) $((\sqrt{83})/83) \langle 5, -3, 7 \rangle$
 (b) $-10((\sqrt{83})/83) \langle 5, -3, 7 \rangle$
 6. (a) $\sqrt{(17/10)} \langle -1, 0, -3 \rangle$
 (b) $((\sqrt{3})/(2\sqrt{17})) \langle 0, -1, -4 \rangle$
 7. (a) $((\sqrt{59})/\sqrt{30}) \langle 2, -5, -1 \rangle$
 (b) $(-10/\sqrt{17}) \langle -1, 0, 4 \rangle$
 8. (a) $(5/\sqrt{6}) \langle -1, 1, 2 \rangle$
 (b) $(-10/\sqrt{6}) \langle -1, 1, 2 \rangle$
 9. $\pm (1/\sqrt{3}) \langle 1, -2, 1 \rangle$
 10. $\pm 2\sqrt{6}$ 11. 0 or 1
 12. (a) $\alpha = 1, \beta = -1$ (b) $\alpha = 1, \beta = 1$
 14. $\alpha = -\beta/2$
 15. $\alpha = 2, \beta = 4$ or $\alpha = 3, \beta = 5$
 16. $5\alpha + 4\beta = 45$
 17. (a) $(1/3) \langle -3, 1, 10 \rangle$
 (b) $(1/5) \langle -8, 24, 52 \rangle$
 18. $\langle -32, -14, 65 \rangle$
 19. $(1/2) \langle 26, -10, -5 \rangle$
 20. (a) 90° (b) 35.3° (c) 85.3° (d) 52.8°
 21. (a) perpendicular (b) Neither
 (c) Parallel, opposite direction
 (d) Parallel, same direction
 22. (a) $(5/\sqrt{13}) \langle 0, 3, 2 \rangle$ or equivalent.
 (b) $(100/\sqrt{2}) \langle 1, 0, 1 \rangle$ or equivalent.
 (c) $(10/\sqrt{5}) \langle 2, 0, 1 \rangle$ or equivalent.
 (d) $(20/3) \langle 2, 2, 1 \rangle$ or equivalent.
 23. $a = b = \sqrt{5}$ 24. $a = -9/8, b = 4$

25. $a = (\sqrt{2})/2, b = \pm (\sqrt{2})/2$
 27. (a) $(1/3) \langle 2, 2, -1 \rangle$ (b) $\langle 1, 1, 1 \rangle$
 28. (a) $(-5/9) \langle 2, -1, -2 \rangle$
 (b) $\langle 0, 1, 2 \rangle$
 29. $(1/16) \langle -5, 18, -7\sqrt{3} \rangle$
 30. $(1/9) \langle -2, 16, 28 \rangle$
 31. (a) $\langle 1, -1, 1 \rangle, \langle 0, 0, 0 \rangle$
 (b) $\langle 1, -1, 1 \rangle, \langle 0, 0, 0 \rangle$
 32. (a) $\langle 2, 1, 3 \rangle, \langle 3, -9, 1 \rangle$
 (b) $\langle 3, -9, 1 \rangle, \langle 2, 1, 3 \rangle$
 33. $\sqrt{(38/51)}$ 34. $(\sqrt{5})/6$
 35. $(\sqrt{2})/2$

Exercise 6.2

3. (a) $\langle 5, 4, -7 \rangle$ (b) $\langle -6, -15, -8 \rangle$
 4. $[(\sqrt{3})/3] \langle 1, -1, 1 \rangle$ 5. $(10\sqrt{3}) \langle 1, -1, -1 \rangle$
 6. (a) $a = 1, b = -1$ (b) $m = 2, n = 2$
 (c) $a = 3, b = -2$ (d) $a = 3, b = -4$
 7. 40 8. 4 9. 18
 10. (a) $(\sqrt{219})/15$ (b) $(\sqrt{154})/77$
 11. $(\sqrt{2})/10$ 12. (a) $10\sqrt{2}$ (b) $5\sqrt{2}$
 13. (a) $2\sqrt{77}$ (b) $\sqrt{77}$

Exercise 7.1

1. (a) $r = \langle 2, 1, 0 \rangle + \lambda \langle 4, 5, -1 \rangle$
 (b) $r = \langle 0, 0, 5 \rangle + \lambda \langle 0, 2, -1 \rangle$
 (c) $r = \langle 1, 1, -1 \rangle + \lambda \langle 1, 2, -1 \rangle$
 (d) $r = \langle \sqrt{2}, 0, 1 \rangle + \lambda \langle 0, -1, 1/5 \rangle$
 2. Equivalent answers including:
 (a) $r = \langle 0, -2, 0 \rangle + \lambda \langle 0, -2, -2 \rangle$
 (b) $r = \langle 1, 2, 1 \rangle + \lambda \langle -2, -3, 3 \rangle$
 (c) $r = \langle 1, 2, 5 \rangle + \lambda \langle 3, 1, -2 \rangle$
 (d) $r = \langle 0.5, -0.1, 0.4 \rangle + \lambda \langle 0.1, 0.4, 0.3 \rangle$
 3. (a) $\lambda = 2$ (b) $\lambda = -5$
 4. $m = 4$ 5. $m = 4$
 6. $\langle 13, -2, 11 \rangle$ is the only point not on the line
 7. (a) $r = \langle 0, 3 \rangle + \lambda \langle 1, -2 \rangle$
 (b) $r = \langle 0, -1 \rangle + \lambda \langle 3, 4 \rangle$
 (c) $r = \langle 0, 3 \rangle + \lambda \langle 4, -3 \rangle$
 8. Gradient = -3 ; $y = -3x + 6$
 9. $x = 3 + \lambda, y = 1 - 2\lambda; 2x + y = 7$
 10. (a) $r = \langle -1, 2, 0 \rangle + \lambda \langle 1, -3, 0 \rangle$
 (b) $r = \langle 1, 2, 4 \rangle + \lambda \langle 2, -1, -1 \rangle$
 (c) $r = \langle 1, -4, 5 \rangle + \lambda \langle 1, 1, 3 \rangle$
 (d) $r = \langle 0, 2, 10 \rangle + \lambda \langle 6, 1, 1 \rangle$
 11. (a) $(x-5)/2 = (y+2)/(-3) = (z+1)/5$
 (b) $(x+1)/(-2) = y-5 = (z-3)/(-4)$
 (c) $(4x-3)/2 = (3y+2)/(-2) = 4z/5$
 (d) $3(x-1)/2 = -5(y+1) = 5(z+1)/3$
 12. (a) $(x+1) = (y+2)/(-3) = (z-2)/6$
 (b) $(x+1)/(-2) = (y+5)/5 = (z-6)/(-2)$
 13. (a) $x = y = z$
 (b) $(x+1)/(-6) = (y-3)/(-3) = (z-4)/(8)$
 (c) $(x-3) = (z+1)/(-2), y = 4$
 (d) $x = 10, z = -5$

14. (a) $r = \langle \lambda, 2 + 5\lambda, 3 - 2\lambda \rangle$
 (b) $r = \langle 0, -1 - \lambda, 5 + 3\lambda \rangle$
 (c) $r = \langle (-1 - 3\lambda)/2, (-1 - 4\lambda)/2, (-5 + 5\lambda)/3 \rangle$
 (d) $r = \langle 1 + 5\lambda/4, (1 - 6\lambda)/3, -(2 - 3\lambda)/6 \rangle$
 15. $r = \langle 1, 2, 3 \rangle + \lambda \langle 5, -2, 0 \rangle$ or equivalent
 16. $r = \langle 2, 2, -2 \rangle + \lambda \langle 1, -2, 0 \rangle$ or equivalent
 17. (a) $x = a + \lambda u, y = b + \lambda v, z = c + \lambda w$
 (b) $\lambda = (x - a)/u = (y - b)/v = (z - c)/w$
 18. (a) Lines intersect at $\langle 13, 17, 4 \rangle$.
 (b) Lines do not intersect.
 19. $m \neq -7$ 20. $m = (-3n + 22)/(n - 6)$
 21. (a) 90° (b) 65.9°
 22. $r = \langle 1, 2, 1 \rangle + \lambda \langle 2, 2, 1 \rangle$ or equivalent

Exercise 7.2

1. (a) -2 (b) 4 (c) $-34/5$ (d) ± 5
 2. (a) No (b) No (c) Yes (d) No
 3. (a) $r \cdot \langle 2, -3 \rangle = -19$
 (b) $r \cdot \langle -5, 10 \rangle = -50$
 (c) $r \cdot \langle 10, 3 \rangle = -16$ or equivalent
 (d) $r \cdot \langle 5, -4 \rangle = 58$ or equivalent
 4. (a) $r \cdot \langle 6, 1 \rangle = 17$
 (b) $r \cdot \langle 3, -4 \rangle = -36$
 (c) $r \cdot \langle 8, -3 \rangle = -81$ or equivalent
 (d) $r \cdot \langle 7, 2 \rangle = 31$ or equivalent
 5. (a) $r \cdot \langle 1, 2 \rangle = 20$
 (b) $r \cdot \langle -4, 3 \rangle = 0.7$
 (c) $r \cdot \langle 3, 10 \rangle = -155$ or equivalent
 (d) $r \cdot \langle -2.7, 0.8 \rangle = 2.27$ or equivalent
 6. (a) $r = \langle 0, -6 \rangle + \lambda \langle 2, 1 \rangle$ or equivalent
 (b) $r = \langle -2, 0 \rangle + \lambda \langle 8, -5 \rangle$ or equivalent
 (c) $r = \langle -5, 0 \rangle + \lambda \langle 4, \sqrt{3} \rangle$ or equivalent
 7. (a) No intersection (b) No intersection
 (c) $\langle 5, 7 \rangle$ (d) $\langle -2, 0 \rangle$
 8. (a) 0° (b) 45°

Exercise 7.3

1. (a) -16 (b) $-9/8$ (c) $-3/2$ (d) $-6/5$
 2. (a) Only $\langle 2, 2, 4 \rangle$ is on the plane.
 (b) Both points are not on the plane.
 3. (a) $r \cdot \langle 4, 0, 3 \rangle = 5$
 (b) $r \cdot \langle -3, 7, 10 \rangle = 26$
 (c) $r \cdot \langle 1, 4, 1 \rangle = 33$
 (d) $r \cdot \langle 4, 8, -11 \rangle = -120$
 4. (a) $r \cdot \langle -1, 0, 2 \rangle = -11$
 (b) $r \cdot \langle 3, -2, -2 \rangle = 23$
 (c) $r \cdot \langle -4, 7, 9 \rangle = -17$
 (d) $r \cdot \langle 1, 10, -10 \rangle = -27/4$
 5. (a) $\langle 0, 4, -8 \rangle$ (b) $\langle 8, 11, -1 \rangle$
 (c) $\langle -1, 8, -7 \rangle$ (d) $\langle -15/2, 5, -21/4 \rangle$
 6. Equivalent answers including:
 (a) (i) $r \cdot \langle 1, 0, 0 \rangle = 0$
 (ii) $r = \lambda \langle 0, 1, 0 \rangle + \mu \langle 0, 0, 1 \rangle$
 (b) (i) $r \cdot \langle 1, 1, 1 \rangle = 8$
 (ii) $r = \langle 1, 2, 5 \rangle + \lambda \langle 4, 0, -4 \rangle$
 $+ \mu \langle 1, -1, 0 \rangle$

6. (c) (i) $r \cdot \langle 1, -1, 1 \rangle = -1$
 (ii) $r = \langle -2, 3, 4 \rangle + \lambda \langle -5, -7, -2 \rangle$
 $+ \mu \langle 8, 0, -8 \rangle$
 (d) (i) $r \cdot \langle -67, 11, -12 \rangle = -254$
 (ii) $r = \langle 4, 10, 8 \rangle + \lambda \langle 2, -2, -13 \rangle$
 $+ \mu \langle -1, -5, 1 \rangle$

7. Equivalent answers including:

- (a) $r \cdot \langle -4, -2, 1 \rangle = 3$
 (b) $r \cdot \langle -11, -38, 13 \rangle = -72$

8. Equivalent answers including:

- (a) $r \cdot \langle 0, 2, 1 \rangle = -1$
 (b) $r \cdot \langle -28, 5, 21 \rangle = 45$

9. (a) $r \cdot \langle 2, 8, 9 \rangle = -27$

- (b) $r \cdot \langle -6, 3, 1 \rangle = 11$

10. Equivalent answers including:

- (a) $r \cdot \langle 6, 0, 1 \rangle = 27$

- (b) $r \cdot \langle 2, -1, 0 \rangle = -13$

11. (a) $3z = 5$ (b) $-2y = 5$

- (c) $-2x - 4y + 3z = 10$

- (d) $5x + 2y - 6z = 25$

12. (a) $r \cdot \langle 1, 0, 0 \rangle = 5$

- (b) $r \cdot \langle 1, 1, 0 \rangle = 1$

- (c) $r \cdot \langle 0, 1, 1 \rangle = 6$

- (d) $r \cdot \langle 2, -3, 4 \rangle = 8$

13. $\langle 19, -3, -21 \rangle$

Exercise 7.4

1. (a) 53.1° (b) 22.2° (c) 20.9° (d) 32.6°
 2. 0.57 or 7.43 3. 1.05 or 19.75
 4. $r = \langle 3 + 5\lambda, 2 + 2\lambda, -1 - 8\lambda \rangle$
 5. (a) 90° (b) 90° (c) 76.1° (d) 87.9°
 6. -0.79 or 58.29 7. -19.62 or 3.62
 8. $m = 2 \pm \sqrt{n^2 + 3}$ 9. 55.5°
 10. $r \cdot \langle 1, -3, 0 \rangle = -1$ or equivalent

Exercise 7.5

1. (a) $|r - \langle 3, 4, 0 \rangle| = 3;$
 $\frac{(x-3)^2}{2} + \frac{(y-4)^2}{2} + z^2 = 9$
 (b) $|r - \langle -1, 2, 2 \rangle| = 5;$
 $\frac{(x+1)^2}{2} + \frac{(y-2)^2}{2} + \frac{(z-2)^2}{2} = 25$
 (c) $|r - \langle -1, 2, -5 \rangle| = \sqrt{10};$
 $\frac{(x+1)^2}{2} + \frac{(y-2)^2}{2} + \frac{(z+5)^2}{2} = 10$
 (b) $|r - \langle 1, 4, -5 \rangle| = 4;$
 $\frac{(x-1)^2}{2} + \frac{(y-4)^2}{2} + \frac{(z+5)^2}{2} = 16$

2. $2\sqrt{2}$

3. $\langle 1, 2, 1 \rangle$ or $(-1/3) \langle 11, 8, 11 \rangle$

4. (a) Outside (b) Inside

5. (a) $|r - \langle -1, 2, -3 \rangle| = 5$

- (b) $|r - \langle 1/2, 3/2, 1 \rangle| = (5\sqrt{6})/6$

6. (a) $\langle 1, 6, 0 \rangle$ or $(1/3) \langle -8, -4, 11 \rangle$

- (b) $\langle 5, -3, -2 \rangle$ or $(1/3) \langle -5, 11, 14 \rangle$

9. $|r - \langle -2, 2, -3 \rangle| = \sqrt{26}$

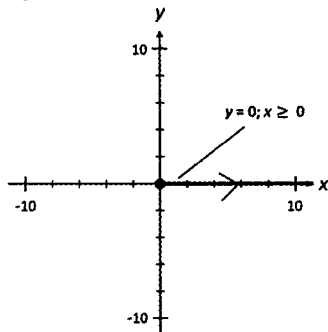
10. (a) Circle with equation $y^2 + z^2 = 64$
 (b) No intersection.
11. (a) Circle with equation $y^2 + z^2 = 99/4$
 (b) At the point $(1, 0, 5)$

Exercise 7.6

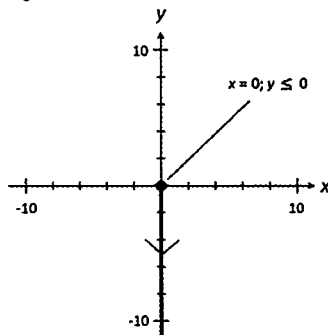
1. (a) $(2\sqrt{357})/17$ (b) $(\sqrt{445})/5$
 (c) $(3\sqrt{2310})/35$ (d) $(3\sqrt{2})/2$
2. $k = 7$ or -13 3. $k = 0$ or -6
4. (b) $\sqrt{5}$ 5. (b) $(2\sqrt{138})/69$
6. (a) $(3\sqrt{21})/7$ (b) $(13\sqrt{42})/21$
7. (a) 2 (b) 2
 (c) 1 (d) 5
 (e) $5\sqrt{6}$ (f) 6
8. $2 \pm 10\sqrt{6}$ 9. $-2/3$
10. (a) $\sqrt{10}$ (b) $\sqrt{2}$
11. $2/3$ 12. 3
13. $1/3$ 14. $(3\sqrt{14})/14$

Exercise 8.1

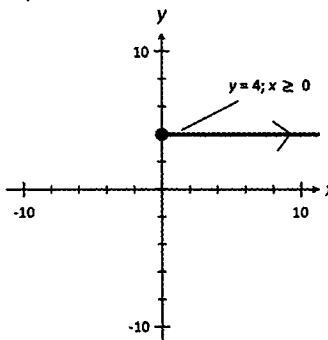
1. (a) $y = 0$



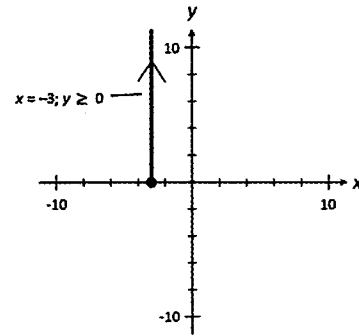
- (b) $x = 0$



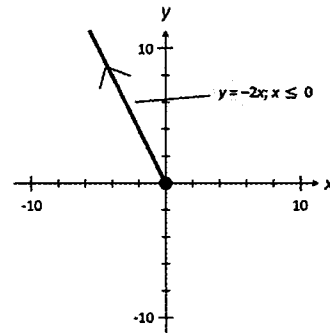
- (c) $y = 4$



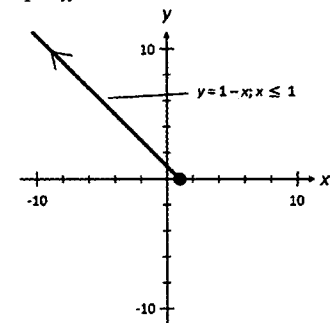
1. (d) $x = -3$



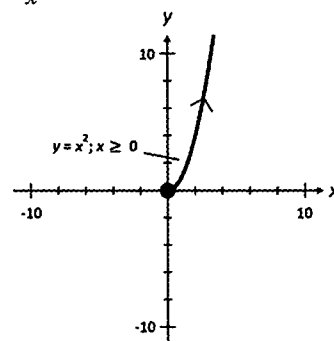
- (e) $y = -2x$



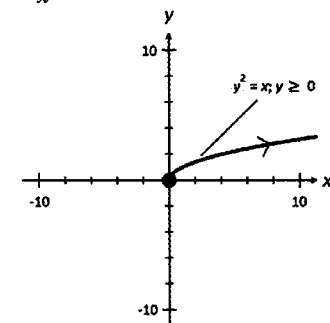
- (f) $y = 1 - x$



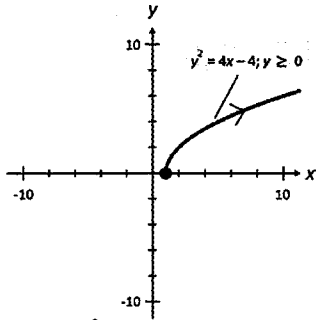
- (g) $y = x^2$



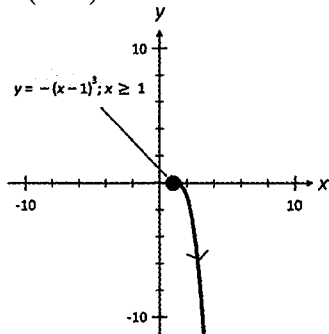
- (h) $y^2 = x$



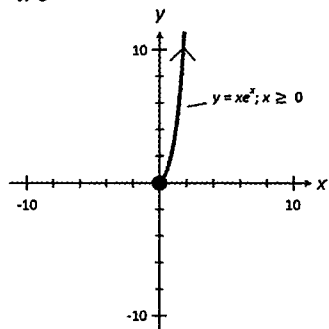
1. (i) $y^2 = 4x - 4$



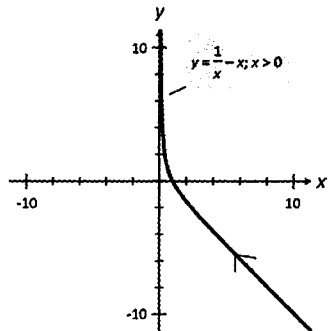
(j) $y = -(x-1)^3$



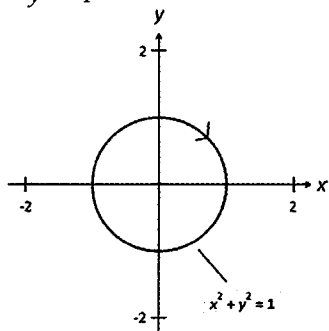
(k) $y = x e^x$



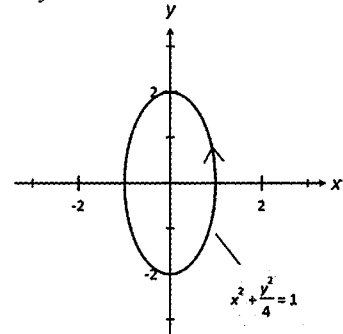
(l) $y = -x + 1/x$



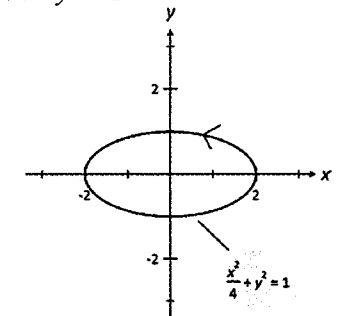
2. (a) $x^2 + y^2 = 1$



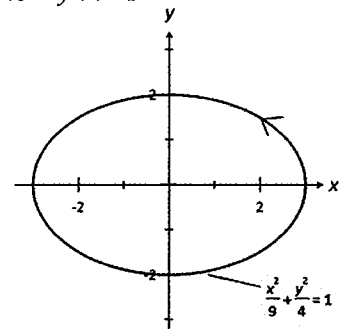
2. (b) $x^2 + y^2/4 = 1$



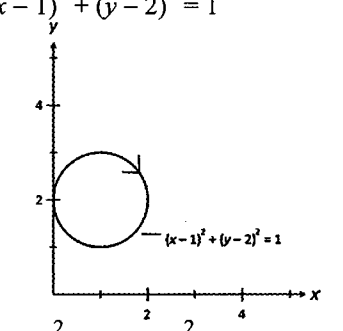
(c) $x^2/4 + y^2 = 1$



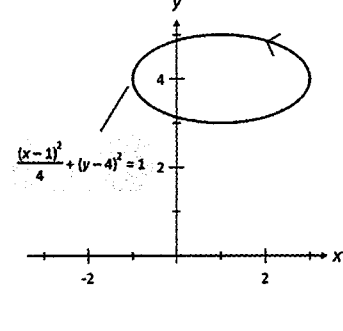
(d) $x^2/9 + y^2/4 = 1$



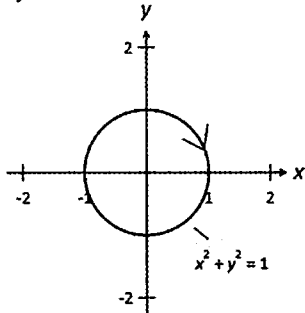
(e) $(x-1)^2 + (y-2)^2 = 1$



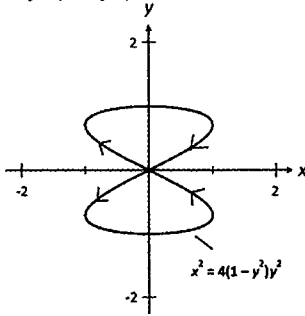
(f) $(x-1)^2/4 + (y-4)^2 = 1$



2. (g) $x^2 + y^2 = 1$



(h) $x^2 = 4y(1-y)$



Exercise 8.2

1. (a) Collide at $t = 2$
 (b) Path of A: $r = \lambda < 1, -2 >$
 Path of B: $r = < 2, -9 > + \mu < 2, 1 >$
 Intersect at $< 4, -8 >$.
2. (a) Do not collide.
 (b) Path of P: $r = < 0, 1 > + \lambda < 1, 1 >$
 Path of Q: $r = < -1, 0 > + \mu < 2, 3 >$
 Intersect at $< -1, 0 >$.
3. (a) $< 5 + t, 2 + t, -10 + 5t > \text{m}$
 (b) 20.8 sec (c) 25.0 sec
4. (a) $a = -5, b = 10, c = -15$ (b) 10 am
5. (a) 5.1 sec and 6.1 sec after 0800 hrs
 (b) 134.4 m, 5.6 sec after 0800 hours.
6. (a) 563.8 m, 0.5 sec before 1 pm
 (b) 3.9 sec before 1 pm and 2.8 sec after 1 pm
7. (a) $\mathbf{OA}(t) = < 100 + 10t, 90 - 40t, 80 + 60t > \text{m}$
 $\mathbf{OB}(t) = < -200 + 22t, 150 - 42.4t, -80 + 66.4t > \text{m}$
 (b) Collide 25 sec after 0800 hours at $< 350, -910, 1580 > \text{m}$.
8. Collision at 6.45 am at $< -5, 110, 0.8 > \text{km}$
9. Interception at 4.30 pm at $< 225, 105, 4.7 > \text{nm}$
10. A and C will collide at 11 am at $< 25, 21, 10 >$.
11. (a) $< x - 4, y - 6, z + 0.15 > \text{ms}^{-1}$
 (b) $< 800, -800, -40 > \text{m}$
 (c) $x = 5, y = 5, z = -0.2$
12. $x = 0.49, y = 3.12, z = -0.12$
13. (a) No intersection. (b) $< -10, 5, 10 >$
 (c) $< 10, 0, 4 >$ (d) No intersection.
14. The two vehicles do not collide.
 Their paths do not intersect.
15. The two vehicles do not collide.
 Their paths intersect at $< 430, 410, 10.9 > \text{m}$.

Exercise 9.1

Please refer to Solution Manual for this text.

Exercise 9.2

Please refer to Solution Manual for this text.

Exercise 10.1

1. (a) $x = 4, y = 1, z = 2$
 (b) $x = 1, y = 2, z = 3$
 (c) $x = 1, y = 4, z = -2$
 (d) $x = 3, y = 3, z = 3$
 (e) $x = 2, y = 1, z = 1$
 (f) $x = -3, y = -4, z = 6$
 (g) $x = 1, y = 2, z = 4$
 (h) $x = -1, y = 2, z = -5$
 (i) $x = -2, y = 12, z = 2$
2. (a) $x = 5, y = 6, z = 1$
 (b) $x = -2, y = 4, z = 3$
 (c) $x = 1, y = 2, z = 3$
 (d) $x = 1/2, y = 1/2, z = -5/8$
3. (a) $x = 2, y = 4, z = -1$
 (b) $x = 3, y = -4, z = 3$
 (c) $x = 3, y = 9/2, z = 9/2$
 (d) $x = 5/2, y = 1, z = 1/4$
4. (a) $x = 4/5, y = 4/5, z = 4/5$
 (b) $x = 5, y = 10, z = 20$
 (c) $x = -1, y = -1, z = 1/2$
 (d) $x = \pm\sqrt{3}, y = \pm\sqrt{2}, z = \pm 1$
5. (a) $x = 1, y = 2, z = -4$ (b) No solution.

Exercise 10.2

1. A costs \$4.90, B costs \$3.90, C costs \$6.50
2. 15 P type, 14 Q type, 13 R type houses
3. 70 of A, 100 of B and 120 of C
4. NBL final \$32, AFL final \$18, Concert \$27
5. (a) 20 of P, 15 of Q, 25 of R
 (b) 4 of P, 3 of Q, 5 of R
6. 10 of A, 15 of B and 18 of C
7. $x = 70, y = 80, z = 60$
8. $x = 5, y = 1, z = 3$
9. 500 of 0 – 1 years, 1700 of 2 – 8 years and 200 of 9 – 10 years
10. (a) 2 red bricks, 8 white bricks, 20 blue bricks
 (b) 1005 of A, 620 of B, 750 of C
11. Any reasonable whole number for n .
12. (a) $x = 20, y = 40, z = 50$
 (b) Loop flow between the junctions C, D and B.
 (c) $k = -11.2$ litres/hour
13. $< t + 4, -t - 1, t > \quad t \in \mathbb{R}$
14. $< 2t + 13, t + 6, t > \quad t \in \mathbb{R}$

Exercise 10.3

1. (a) Equations 1 & 2 inconsistent.
 (b) Equation 1 + Equation 2 inconsistent with Equation 3.
 (c) Equations 1 & 2 inconsistent.
 (d) Equation 2 – Equation 1 inconsistent with Equation 3.

2. (a) Equations 1 & 2 are identical.
 (b) Equation 1 – Equation 2 similar to Equation 3.
 (c) $2 \times$ Equation 1 + Equation 2 similar to Equation 3.
 (d) Equation 2 – Equation 1 similar to Equation 3.
3. (a) (i) $p \neq 0, q$ any no. (ii) $p = 0, q \neq 1$
 (iii) $p = 0, q = 1$
 (b) (i) $p \neq 3, q$ any no. (ii) $p = 3, q \neq \frac{1}{2}$
 (iii) $p = 3, q = \frac{1}{2}$
 (c) (i) $p \neq -1$ (ii) $p = -1$
 (iii) No value for p
 (d) (i) $p \neq 1, p \neq -2$; any real number for q
 (ii) $p = 1$ and $q \neq 1$ or $p = -2$ and $q \neq 1$
 (iii) $p = 1$ and $q = 1$ or $p = -2$ and $q = 1$
 (e) (i) $p \neq -1$ and $p \neq -2$
 (ii) $p = -1$ (iii) $p = -2$
 (f) (i) $p \neq 3$ (ii) No value for p
 (iii) $p = 3$
4. (a) System will always have no solutions.
 (b) (i) System will always have solutions.
 (ii) $k \neq 4, k \in \mathbb{R}$
 $x = 19/7, y = -11/7, z = 0$
 (iii) $k = 4$
 $x = (19 - t)/7, y = (5t - 11)/7$
 $z = t, t \in \mathbb{R}$
 (c) (i) System will always have solutions.
 (ii) $k \neq 7, k \in \mathbb{R}$
 $x = 0, y = -1, z = 2$
 (iii) $k = 7$
 $x = (14 - 7t)/19, y = (3 - 11t)/19$
 $z = t, t \in \mathbb{R}$
 (d) (i) $k \neq -5, k \in \mathbb{R}$
 (ii) Not possible.
 (iii) $k = -5$
 $x = 1 - t, y = 1 - t, z = t, t \in \mathbb{R}$
5. $k = 5/4, 2$ 6. $a = 9, b = 1$

7. (a)
$$\left(\begin{array}{ccc|c} 1 & 3 & 1 & 16 \\ 1 & 4 & 3 & 23 \\ 1 & 2 & 4 & 19 \\ 1 & 5 & 3 & p \end{array} \right)$$

(b) Variations possible,

$$\left(\begin{array}{ccc|c} 1 & 3 & 1 & 16 \\ 0 & -1 & -2 & -7 \\ 0 & 0 & -5 & -10 \\ 0 & 0 & -2 & -30+p \end{array} \right)$$

- (c) $p = 26$
8. (a) $k = 1$
 (b) $k = -2$
 $x_1 = -5 + 4t, x_2 = 8 - 6t, x_3 = t, x_4 = 5 - 4t$
 (c) $k \neq 1$ and $k \neq -2, k \in \mathbb{R}$
 $x_1 = (k + 1)/(1 - k), x_2 = (2k + 1)/(k - 1),$
 $x_3 = (2k - 3)/(2k - 2), x_4 = (k + 1)/(k - 1)$

9.
$$\frac{1}{3} \begin{pmatrix} 2 & 1 & 1 \\ -1 & 1 & 1 \\ -2 & -1 & 2 \end{pmatrix}$$

Exercise 11.1

1. (a) $[(-2/\sqrt{x})]/(1 - \sqrt{x})^3$
 (b) $e^{-x}/\sqrt{(1 - 2e^{-x})}$
 (c) $2(\cos x - 2 \sin 2x)(\sin x + \cos 2x)$
 (d) $1/[2(1+x)\sqrt{(1 + \ln(1+x))}]$
 (e) $-\sec x e^{-\tan x}$
 (f) $\pi \sin 2(1 + \pi x)$
 (g) $(-\pi \sin \pi x)/(1 + \cos \pi x)$
 (h) $-2(x - 1)e^{-(x-1)^2}$
 (i) $-8x/(1 - x)^2$
 (j) $(-\operatorname{cosec}(1 + \sqrt{x})/(-2\sqrt{x}))$
 (k) $e^{1+x} \sec(e^{1+x}) \tan(e^{1+x})$
 (l) $2x 2^{1+x^2} \ln 2$
2. (a) $2x \sin \omega x + \omega x^2 \cos \omega x$
 (b) $(1/(2\sqrt{x}))e^{\cot x} - (\sqrt{x}) \operatorname{cosec} x e^{2 \cot x}$
 (c) $4(1 + 2x) \tan \omega x + 2\omega x (1 + 2x)^2 \sec^2 \omega x$
 (d) $2(x + 1)e^{(x+1)^2} \ln \cos^2 x - 2e^{(x+1)^2} \tan x$
 (e) $(\sin x \sin \pi x)e^{2 - \cos x} + (\pi \sin 2\pi x)e^{-\cos x}$
 (f) $-2 \sin 2x \sin^2 x + (\sin 4x)/2$
 (g) $1/x + (\sec x)/(\tan x)$
 (h) $-2xe^{-x^2} (\ln x + 2x) + e^{-x^2} (1/x + 2)$
 (i) $x \ln(1 + e^x) + (x^2 e^x)/(2(1 + e^x))$
 (j) $2/x - 1/(1 + x)$
 (k) $e^{1+x} [\ln 2x - \ln(1 - x)]$
 $+ e^{1+x} (1/x + 1/(1 - x))$
 (l) $2x [\ln x - 2x - 2 \ln(1 + x)]$
 $+ x^2 [1/x - 2 - 2/(1 + x)]$
3. (a) $\frac{2x(1 - 2x) + 2(1 + x^2)}{(1 - 2x)^2}$
 (b) $\frac{1}{2\sqrt{x}(1 + \sqrt{x})^2}$
 (c) $2/(1 + \cos 2x)$
 (d) $\frac{2e^{2x} + 4}{(1 + 2e^{-2x})^2}$
 (e) $\frac{e^{-2\cos x} (2 \sin x - 4e^{\sin x} \sin x + 2e^{\sin x} \cos x)}{(1 - 2e^{\sin x})^2}$

3. (f) $[1 - \ln(1 + 2x)]/(1 + 2x)^2$
 (g) $\frac{2x(1 + e^{2x})\ln(1 + e^{2x}) - 2x^2 e^{2x}}{(1 + e^{2x})[\ln(1 + e^{2x})]^2}$
 (h) $\frac{e^{\sin x}(\cos x + e^{-\cos x} \cos x - e^{-\cos x} \sin x)}{(1 + e^{-\cos x})^2}$
 (i) $\frac{e^x}{(1 + e^x)^2} \sec^2 \frac{e^x}{(1 + e^x)}$
 (j) $\frac{-e^{\left(\frac{x}{x-1}\right)}}{(x-1)^2}$ (k) $\frac{-e^{\left(\frac{\cos x}{1+\sin x}\right)}}{(1 + \sin x)}$
 (l) $\frac{x(1 - \ln(1 + x^2))}{(1 + x)^2}$
4. (a) $\frac{3}{2\sqrt{x}} + 3 + \frac{3\sqrt{x}}{2}, \frac{-3}{4x^{3/2}} + \frac{3}{4\sqrt{x}}$
 (b) $\frac{e^{-x}}{2}(1 - e^{-x})^{-1/2}, \frac{-e^{-x}}{4}(1 - e^{-x})^{-3/2}(2 - e^{-x})$
 (c) $-2 \sin 4x, -8 \cos 4x$
 (d) $1/(1 + x), -1/(1 + x)^2$
 (e) $-e^{-\sin x} \cos x, e^{-\sin x} (\sin x + \cos x)^2$
 (f) $2 \tan x + 2 \tan^2 x, 2 + 8 \tan x + 6 \tan^2 x$
5. $4(x + 2) \cos x - (x^2 + 4x - 1) \sin x$

Exercise 11.2

1. (a) $6(x - 1)$ (b) $-2/x^3$
 (c) $(x - 1)/(2x^{3/2})$ (d) $\pm 1/\sqrt{x}$
2. (a) $(2t^2 - 1)/(t^2 + 1)$ (b) $(6t - 1)/(6t^2 + 1)$
 (c) $(t^2 + 1)/(t^2 - 1)$ (d) $(1 - t)/(1 - 2t)^2$
3. (a) $\pm x/\sqrt[2/3]{(4 - x^2)}$ (b) $\pm (x - 2)/\sqrt[1/3]{(4x - x^2)}$
 (c) $\pm[\sqrt[1/3]{(1 - x^2)}]/x$ (d) $-4x$

Exercise 11.3

1. (a) $-(2x + 3y)/(3x + 2y)$
 (b) $(2x - y)/(x + 2y)$
 (c) $(1 - y - 2xy)/(x + 2xy)$
 (d) $-(y + 4x^{3/2} y^{1/2})/(x + 4y^{3/2} x^{1/2})$
 (e) $-(e^y + ye^x)/(e^x + xe^y - 1)$
 (f) $y(4 - y - 2x \ln y)/(x^2 + xy)$
2. (a) $[2x \cos y + y \cos x]/[x^2 \sin y - \sin x]$
 (b) $\frac{\sin y \sin x - e^{\cos y}}{\cos y \cos x - x \sin y e^{\cos y}}$

2. (c) $\frac{3 + y \sin xy - 4 \tan y}{4x \sec^2 y - x \sin xy}$
 (d) $y/[e^{y/2} \sin(e^{y/2}) - x - \cot(y)]$
 (e) $-y/[x(1 + y e^{y/2})]$
 (f) $-(y^2 + 2y - 1)/[x(y + 1)]$
3. (a) $2x(dx/dt) + 2y(dy/dt)$
 (b) $\cos x(dx/dt) - \sin y(dy/dt)$
 (c) $-2e^{-2x}(dx/dt) + 0.05e^{0.05y}(dy/dt)$
 (d) $2xy(dx/dt) + x^2(dy/dt)$
 (e) $e^{-x} \sin \pi y(dx/dt) + \pi e^{-x} \cos \pi y(dy/dt)$
 (f) $\ln(1 + \tan y)(dx/dt) + [(x \sec^2 y)/(1 + \tan y)](dy/dt)$
 (g) $(1/y)(dx/dt) - (x/y)(dy/dt)$
 (h) $e^{2x}(1 - e^{-y})[2(dx/dt) + e^{-y}(dy/dt)]/(1 + e^{-y})^2$
 (i) $[(1 + \cos x) \cos y(dy/dt) + \sin x \sin y(dx/dt)]/(1 + \cos x)^2$

Exercise 11.4

1. (a) $2^x \ln(2)$ (b) $x^x [1 + \ln x]$
 (c) $2^{2x+1} \ln 2$ (d) $2x^{\ln(x)-1} \ln(x)$
 (e) $x^{\sin x} \{\cos(x) \ln(x) + [\sin(x)]/x\}$
 (f) $x^{\cos x} \{[\cos(x)]/x - \sin(x) \ln(x)\}$
 (g) $(1 + x)^x \{\ln(1 + x) + x/(1 + x)\}$
 (h) $-(1/x)^x [\ln(x) + 1]$
 (i) $[(\ln x)^{\ln x}][\ln(\ln(x) + 1)]/x$
2. (a) $2/(1 - x)^2$
 (b) $(x^4 + 3x^3 + 2x^2)/(1 - x)^{3/2}$
 (c) $(-x^4 + 2x^3 + 3x^2 - 2x + 1)/(1 - x)^{3/2}$
 (d) $(1 + x)(-2x^2 + 6x + 4)/(1 - 2x)^{3/2}$
 (e) $-2(1 - 2x)(8 - x)/(x + 2)$
 (f) $-(2 + \sqrt{x})(\sqrt{x} + 8)/[2\sqrt{x}(\sqrt{x} - 1)^4]$
 (g) $1/[(2x)^{1/2} (1 - 3x)^{3/2}]$
 (h) $1/[2(1 + x)^{1/2} (3x + 4)^{3/2}]$
 (i) $2x/[(1 + x)^{1/2} (1 - x)^{3/2}]$

Exercise 12.1

1. (a) $y = -x + 1$
 (b) $y = -2x/3 + 2/3; y = 2x/3 - 11/3$
 (c) $y = -x/2 + \pi/3$
 (d) $y = -x/2 - 3/2$
2. $y = -x + 1$ 3. $y = -12x + 3$
4. $(-2, 0)$ & $(2, -2)$ 5. $(2, -2)$ & $(-2, 2)$
6. $(1, -1)$ & $(-1, 1)$

7. $(1, 2n\pi), (-1, (2n+1)\pi)$
 & $(0, (4n+1)\pi/2)$ for $n \in \mathbb{Z}$
 8. (a) $y = -2$ (b) $x = -2$
 9. (a) $x = -2$ (b) $y = 0, y = 3/2$
 10. (a) $x = \pm \pi\sqrt{-(4n+1)}$ for $n \in \mathbb{Z}^-$
 (b) $y = -0.7391$

Exercise 12.2

1. 0.1 2. -2.5
 3. (a) $3/20$ (b) $(\sqrt{3})/10$
 4. (a) $-\frac{\pi\sqrt{3}}{2^{-1}}$ (b) $-\frac{6\sqrt{3}}{\pi}$
 5. 2 cm s^{-1} ; 0.8 cms^{-1}
 6. 0.031 mms^{-1} ; 0.016 mm s^{-1}
 7. 0.0025 m/min
 8. (a) $4\pi \text{ cm s}^{-1}$ (b) $8\pi \text{ cm s}^{-1}$
 9. 0.032 cms^{-1} ; 63.08 cm s^{-1}
 10. 0.10 m/min 11. -1 cm/min
 12. 0.0019 cm/min 13. -0.031 ms^{-1}
 14. 0.052 ms^{-1} 15. 0.18 ms^{-1}
 16. -22.86 m/min 17. $1/100 \text{ rad/sec.}^{-1}$
 18. $-1/250 \text{ rad/sec}$ 19. 2.4 cms^{-1}
 20. 50.27 cm/min 21. 54.66 km/min
 22. 11.17 ms^{-1} 23. -11.12 ms^{-1}
 24. 26.8 ms^{-1} 25. 0.96 cm/min

Exercise 13.1

1. $x \sin(x) + \cos(x) + C$
 2. $e^x [\sin(x) + \cos(x)]/2 + C$
 3. $2[x \ln(x) - x] + C$
 4. $x e^x - e^x + x^2/2 + C$
 5. $\frac{1}{2} e^{x^2} + C$ 6. $-e^{\cos(x)} + C$
 7. $-\frac{1}{2} [e^x (\sin(x) + \cos(x))] + C$
 8. $-(x+2x+2)e^{-x} + C$
 9. $-e^{-x}(1+x) - x^2/2 + C$
 10. $x^3/3 + x^2 [2 \ln(x) - 1]/4 + C$
 11. (a) $(\sqrt{x+1})^2 + C$ (b) $e^x + C$
 (c) $(\sqrt{x+1})^2 + e^x + C$ (d) $x^2/2 + (\sqrt{x+1})^2 + C$

Exercise 13.2

1. (a) $4\sqrt{x} + C$ (b) $3(\sqrt{x})/2 + C$
 (c) $-1/[4(2t+1)^2] + C$
 (d) $-(1-4x)^{1/2} + C$ (e) $(x+1)^4/4 + C$
 (f) $-1/x - 2/x^2 - 4/(3x^3) + C$
 (g) $x^7/7 + x^4/2 + x + C$
 (h) $t^7/7 - 3t^5/5 + t^3 - t + C$
 2. (a) $(1+x)^{2/4} + C$ (b) $-(1-2x)^{2/3/2} + C$

2. (c) $-(1-x)^{3-3}/3 + C$ (d) $4(1+x)^{3/2} + C$
 (e) $(2x+x^2)^4/8 + C$ (f) $-(2x-x^2)^2/2 + C$
 (g) $(1-1/x)^4/4 + C$ (h) $2(1+\sqrt{x})^5/5 + C$
 3. (a) $8e^{0.05x} + C$ (b) $-5e^{-0.1x} + C$
 (c) $(e^{2x})/2 + C$ (d) $-(e^{-6x})/3 + C$
 (e) $2e^{2x} + 4e^x + x + C$
 (f) $x - e^x + C$
 (g) $(e^{2x})/2 + 4x - 2e^{-2x} + C$
 (h) $-(e^{-2x})/2 + 4x - 4e^{-x} + C$
 4. (a) $\frac{e^{2x^2}}{16} + C$ (b) $\frac{-3e^{-x^2}}{4} + C$
 (c) $\frac{e^{1+x^2}}{2} + C$ (d) $e^{x^2-4} + C$
 (e) $\frac{e^{x^2+2x}}{2} + C$ (f) $\frac{(1+e^x)^5}{5} + C$
 (g) $(1/3)(e^{2x} - 1)^{3/2} + C$
 (h) $(-1/8)(1+2e^x)^{-4} + C$

Exercise 13.3

1. (a) $(2/3) \ln|1+3x| + C$
 (b) $(-4/5) \ln|2-5x| + C$
 (c) $x^2/8 - x + \ln|x| + C$
 (d) $-1/(3x) + 2 \ln|x| + 4x + (4x^2)/3 + C$
 (e) $x - 2 \ln|x| - 1/x + C$
 (f) $x + 3 \ln|x| - 3/x - 1/(2x^2) + C$
 (g) $(-7/6) \ln|1-3x^2| + C$
 (h) $(-1/2) \ln|2x^3 - 1| + C$
 2. (a) $(-1/2) \ln|x^2 - 8x| + C$
 (b) $3 \ln|x^2 + 3x| + C$
 (c) $\ln|1+x| + C$
 (d) $(-5/4) \ln|1+2e^{-2x}| + C$
 (e) $(3/4) \ln|1+2e^{x^2}| + C$
 (f) $(1/2) \ln|e^{2x} + e^{-2x}| + C$
 (g) $6 \ln|1+\sqrt{x}| + C$
 (h) $(-3/2) \ln|1+1/x| + C$
 (i) $\ln|\ln x| + C$
 3. (a) $x^2 + C$ (b) $x^6/3 + C$
 (c) $2x^6/3 + C$ (d) $\sqrt{x+x^2} + C$

Exercise 13.4

- (a) $(\sin 2x)/2 + C$ (b) $\cos(1 - 2t) + C$
 (c) $(\tan(1 + 2x))/2 + C$
 (d) $(-1/\pi) \ln |\cos \pi x| + C$
 (e) $(-3/2) \cot(4t/3) + C$
 (f) $(1/2) \ln |\sin 3x| + C$
 (g) $-((\sqrt{2})/\pi) \cot(1 + \pi t) + C$
 (h) $(5/3\pi) \tan(\pi x + 1) + x/3 + C$
 (i) $(1/(3\pi)) \cot(\pi x) + x/3 + C$
- (a) $(-1/2) \cos^2 2x + C$
 (b) $(-1/4) \sin^2(1 - x) + C$
 (c) $(3/2) \tan^4 x + C$
 (d) $(-1/4) \cot^4 x + C$
 (e) $(1 + \sin x)/4 + C$
 (f) $(1 - 2 \cos 2x)^{3/2}/6 + C$
 (g) $-(1 + \cot x)/4 + C$
 (h) $2(1 + \tan x)^{1/2} + C$
 (i) $(1 + \cot 2x)^{-3}/6 + C$
- (a) $(-1/(2\pi)) \ln |1 - \sin 2\pi x| + C$
 (b) $(-1/2) \ln |1 + \cos(2x + 1)| + C$
 (c) $(-1/2) \ln |\cos 2x - \sin 2\pi x| + C$
 (d) $(1/2) \ln |1 + \tan 2x| + C$
 (e) $(-3/4) \ln |1 + 2 \cot 2x| + C$
 (f) $(-1/2) \ln |1 - 2e^{\sin x}| + C$
- (a) $(1/4) \sin^2 2x + C$
 (b) $(-1/3) \cos 2x + C$
 (c) $(1/2) \sin 2x + C$
 (d) $(1/4) \sin 4x + C$
 (e) $\ln |\sin 2x| + C$
 (f) $(1/2) \tan x + C$
- (a) $(1/2) \tan 2x + C$
 (b) $(1/10) \tan^2 2x + C$
 (c) $(2/3)(1 + \tan x)^{3/2} + C$
 (d) $(-1/4)(1 + 2 \tan x)^{-2} + C$
 (e) $(\pi + \tan 2x)^{1/2} + C$
 (f) $(-1/2) \ln |3 - 2 \tan x| + C$
- (a) $(-1/2) \cot 2x + C$
 (b) $(-1/(5\pi)) \cot^3 \pi x + C$
 (c) $(-2/3)(1 + \cot x)^{3/2} + C$
 (d) $(-1/3)(1 - \cot x)^{-3} + C$
 (e) $(-2/3)(4 + 3 \cot x)^{1/2} + C$
 (f) $-\ln |2 + \cot x| + C$
- (a) $-\cos x + C$ (b) $(\sin 3x)/3 + C$
 (c) $(-1/\pi) \cos(\pi x + \pi/6) + C$
 (d) $(-1/3) \ln |\cos 3x| + C$

- (a) $\cos x + C$ (b) $(\sin^2 x)/2 + C$
 (c) $-\ln |\cos \sqrt{x}| + C$

Exercise 13.5

- (a) $[x - (\sin 8x)/8]/2 + C$
 (b) $(1/4)[3x/2 - (1/\pi) \sin(2\pi x) + (1/8\pi) \sin(4\pi x)] + C$
 (c) $(1/2)\{t - (1/4) \sin[2(1 - 2t)]\} + C$
 (d) $(1/2)\{x + [\sin(4\pi x)]/(4\pi)\} + C$
 (e) $[-1/(2\pi)]\{\cos(2\pi t) - [\cos^2(2\pi t)]/3\} + C$
 (f) $(2/\pi)\{\sin(\pi x/2) - [\sin^3(\pi x/2)]/3\} + C$
 (g) $(-1/\pi)\{\cos(\pi t) - (2/3) \cos^3(\pi t) + (1/5) \cos^5(\pi t)\} + C$
 (h) $(-1/\pi)\{\sin(1 - \pi x) - (1/3) \sin^3(1 - \pi x)\} + C$
 (i) $(2/\pi)\{\cos[1 - (\pi x/2)] - (2/3) \cos^3[1 - (\pi x/2)] + (1/5) \cos^5[1 - (\pi x/2)]\} + C$
- (a) $[1/(2\pi)] \sin(\pi t) + C$
 or $[-1/(4\pi)] \cos(2\pi t) + C$
 (b) $[2/(3\pi)] \sin^3(\pi x/2) + C$
 (c) $[-1/(9\pi)] \cos^6(3\pi x) + C$
 (d) $[1/(3\pi)] \sin(\pi x) + C$
 (e) $(1/8)[x - (\sin 2x)/2] + C$
 (f) $(1/\pi)\{[\sin^3(\pi t)]/3 - [\sin^5(\pi t)]/5\} + C$
 (g) $(-1/2)\{[\cos^2(2x)]/3 - [\cos^4(2x)]/5\} + C$
 (h) $1/\cos(x) + \cos(x) + C$
 (i) $-1/\sin(x) - \sin(x) + C$

Exercise 13.6

- (a) $(1 + 2x)^7/14 + C$
 (b) $-(1 - 2t)^{3/2}/3 + C$
 (c) $4(x + 1)^{3/2}/3 + C$
 (d) $4(1 + x^2)^{3/2}/9 + C$
 (e) $-(9 - 4x^2)^{1/2}/2 + C$
 (f) $4(x - 8)^{1/2}/3 + C$
- (a) $4(4 + \sqrt{x})^{5/3}/5 - 16(4 + \sqrt{x})^{3/2}/3 + C$
 (b) $2(1 + x)^{5/2}/5 - 2(1 + x)^{3/2}/3 + C$
 (c) $(-2/3)(1 - x)^{3/2} + (4/5)(1 - x)^{5/2} - (2/7)(1 - x)^{7/2} + C$
 (d) $(1/32)[2(1 + 2x)^{11/2}/11 + 8(1 + 2x)^{9/2}/9 + 12(1 + 2x)^{7/2}/7 + 8(1 + 2x)^{5/2}/5 + 2(1 + 2x)^{3/2}/3] + C$
 (e) $(1/4)[(2x + 1) - \ln |2x + 1|] + C$
 (f) $(x + 2) - 4 \ln |x + 2| - 5/(x + 2) + C$
 (g) $4(4 + x)^{3/2}/3 - 16(4 + x)^{1/2} + C$
 (h) $2(2 + \sqrt{x} - 2 \ln |2 + \sqrt{x}|) + C$

3. (a) $\sin x^2 + C$
 (b) $(-3 \cos(x^2 + 1))/2 + C$
 (c) $(\tan(2x^2))/4 + C$ (d) $-2 \ln|\cos x^2| + C$
 (e) $(\sin(2x^2 + 1))/4 + C$
 (f) $(-\cos(2 + x^3))/3 + C$
4. (a) $(1 + \sqrt{x})^4/2 + C$ (b) $(1 + \ln|x|)^3/3 + C$
 (c) $[2x + 3 + \ln|2x + 3|]/4 + C$
 (d) $1/(1-x) + 3 \ln|1-x| - (1-x) + C$
 (e) $2(x+9)^{3/2}/3 - 16(x+9)^{1/2} + C$
 (f) $2[(1 + \sqrt{x})^3/2 - 3(1 + \sqrt{x})^2/2 + 3(1 + \sqrt{x}) - \ln|1 + \sqrt{x}|] + C$
 (g) $(-1/2) \cos(x^2) + C$
 (h) $2 \sin(\sqrt{x}) + C$ (i) $\cos(1/x) + C$
 (j) $-\sin(e^{-x}) + C$ (k) $(1/2) \tan(x^2) + C$
 (l) $-1/[3 \tan(x^3)] + C$

Exercise 13.7

1. (a) $-2(4-x)^{2/2} + C$
 (b) $(-1/4)(9-4t)^{-1} + C$
 (c) $\tan^{-1} x + C$
 (d) $(1/15) \tan^{-1}(3x/5) + C$
2. (a) $-\cos^{-1}(x/2) + C$
 (b) $(-1/2) \cos^{-1}(2x/3) + C$
 (c) $[\sin^{-1} x + x \sqrt{(1-x^2)}]/2 + C$
 (d) $-2 \cos^{-1}(x/2) + (x \sqrt{(4-x^2)})/4 + C$
 (e) $-\sqrt{(1-x^2)} - \sin^{-1} x + C$
 (f) $-2\sqrt{(16-x^2)} - \cos^{-1}(x/4) + C$
3. (a) $[\tan x]/3 + [\tan x]^{1/2}/5 + C$
 (b) $(2/3)[3 \tan x + 2]^{1/2} + C$

Exercise 13.8

1. (a) $x - 2 \ln|x+2| + C$
 (b) $x/2 - (5/4) \ln|2x+1| + C$
 (c) $-3x/2 - (1/4) \ln|1-2x| + C$
2. (a) $(1/2) \ln|(x-1)/(x+1)| + C$
 (b) $(3/14) \ln|2x+1| + (2/7) \ln|x-3| + C$
 (c) $(-13/24) \ln|3x+2| - (9/8) \ln|2-x| + C$
 (d) $(-2/3) \ln|2x-1| + (5/3) \ln|x-2| + C$
 (e) $x - (3/5) \ln|x+2| + (8/5) \ln|x-3| + C$
 (f) $(1/2) \ln|x+1| + (1/10) \ln|x-3| - (3/5) \ln|x+2| + C$
3. (a) $\ln|x/(x-1)| - 2/(x-1) + C$
 (b) $3 \ln|x| + 1/x - 3 \ln|x+1| + C$

3. (c) $3 \ln|x+1| + 1/(x+1) - 3 \ln|x+2| + C$
 (d) $x - 1/[2(x-1)] + (5/4) \ln|x-1| - (1/4) \ln|x+1| + C$
 (e) $3/[4(x+2)] + (3/16) \ln|x-2| + (13/16) \ln|x+2| + C$
 (f) $x - 28/[3(x-3)] + (1/9) \ln|x| + (53/9) \ln|x-3| + C$
4. (a) $-\ln|x+1| + (1/2) \ln|x^2+1| + C$
 (b) $-2 \ln|x+1| + \ln|x^2+x+1| + C$
 (c) $\ln|x-1| + \ln|x^2+x-1| + C$

Exercise 14.1

1. (a) $(1/2) \ln(3/2)$ (b) $-5 \ln 2 + 3 \ln 3$
 (c) $4 \ln 3 - 7 \ln 2$
2. (a) $1 + 5 \ln 2 - 4 \ln 3$ (b) $1 + (3/2) \ln 3 - \ln 2$
 (c) $-5/2 + 3 \ln 2 + 2 \ln 3$
3. (a) $-1/2 - 3 \ln 2 + 2 \ln 3$
 (b) $1/8 + (1/4) \ln 2 - (1/4) \ln 3$
 (c) $5/4 + (3/4) \ln 2 + (1/4) \ln 3$
4. (a) $3 \ln 2$ (b) $-4 \ln 2$ (c) $2 \ln 3 - 3 \ln 2$

Exercise 14.2

1. (a) $2[-(2\sqrt{3})/5 + (16\sqrt{2})/15]$
 (b) $2[8 \ln 2 - 4 \ln 3 - 1]$ (c) $2 - \ln 3$
 (d) $-26/3 + (28\sqrt{2})/3$
2. (a) 2 (b) 1 (c) 1/2
3. (a) $\pi/12$ (b) $\pi/18$ (c) $\pi/8$

Exercise 14.3

1. (a) 8/3 (b) 16/3 (c) 8 (d) 1/3
2. (a) 9/8 (b) 2 (c) $2(\sqrt{2}-1)$
 (d) $e^2/2 + 1/e - 3/2$
3. (a) 1/6 (b) 9/2 (c) 13/6 (d) 13/6
4. (a) 2 (b) 9/2 (c) $5/3 - 2 \ln 2$
 (d) $8/3 - 2 \ln 3 + 2 \ln 2$
5. (a) $\pi/8 + (\sqrt{3})/2 - 1$ (b) $(\sqrt{3})/2 + \pi/2$
6. $(1/2)[5 + \ln(45/64)]$
7. 4 8. $8 - \pi/3$ 9. $9\pi/4$
10. (a) 2.9540 (b) 9.8633
 (c) 4.1045 (d) 18.6768
11. (a) 0.6321 (b) 0.8415
 (c) 0.7372 (d) 1.8887
12. (a) 32/3 (b) 9/2
 (c) $(32\sqrt{2})/3$ (d) 16/5
13. (a) $3/4 - 2b + 3b^2/2 - b^4/4$
 (b) $b^4/4 - 3b^2/2 + 2b + 51/4$
 (c) $b^4/4 - 3b^2/2 + 2b + 51/4$

Exercise 14.4

- (a) $16\pi/15$ (b) $512\pi/15$ (c) $16\pi/15$
(d) $\pi/105$ (e) π (f) π
- (a) 3.35 (b) 342.96 (c) 154.57
(d) 17.40 (e) 35.02 (f) 2.47
(g) 9.42 (h) 3.35
- (a) 1.57 (b) 7.33 (c) 0.71
(d) 9.07 (e) 0.52 (f) 7.87
(g) 113.10 (h) 201.06
- (a) 64.72 (b) 37.70 (c) 724.10
(d) 3.14 (e) 40.74

Exercise 15.1

- (a) 1.09 error 0.7%
(b) 1.069 error -1.2%
(c) 1.0807 error -0.16%
- (a) 9.0009 error 0.01%
(b) -68.3344 error 0.0015%
- (a) 0.7469 (b) 0.3103
- (a) 8.7733 (b) 1.4558
- (a) 6.7965 (b) 1.4035

Exercise 16.1

- (a) $y = \ln|x^2 + 1| - 4$
(b) $y = (-1/2)\ln|(x-1)(x+1)^3| + 2$
(c) $y = -4\ln|x+1| + 5\ln|x+2| - 4\ln 2$
(d) $y = -\sin^{-1}(x)$ (e) $y = \tan^{-1}(2x)$
(f) $y = \sin^{-1}(x) + x\sqrt{1-x^2}$
- $y = -2\pi x + \sin(2\pi x)$ 3. $y = \sin^2(x) - 2$
- $y = -12\cos(x) + 4\cos^3(x) + 4$
- $y = 6(x+1)^{5/2} - 10(x+1)^{3/2} + 2$
- $y = -2x + 2\ln|2x+1| + 2$

Exercise 16.2

- (a) $y = 100e^{0.02t}$ (b) $y = 50e^{3t}$
(c) $y = 202e^t - 2$ (d) $y = [4 + 1196e^{-3t}]^3$
(e) $y = [-1 + 501e^{-10t}]^5$
(h) $y = (1/2)(1 + 399e^{-20t})$
- $dy/dt = 0.03y$ with $y(0) = 100\,000$
- $dP/dt = P/3$ with $P(0) = 100\,000$
- 4 620 981 yrs
- 194.34 yrs, 839.91 yrs
- 1.33 rads 7. 0.46g
- (a) 2.23% (b) 0.288%
- (a) $k = 0.067\,29$ (b) 22.9 min
- (a) $k = 0.030\,31$ (b) 81.3 min
- $I = 2(1 - e^{-4t})$ 12. (b) 69.31 min
- (a) $a = 80, b = 25$
(b) $m = 2\,000, n = 1\,500, k = 1/25$
(c) 1.72 min (d) $500 \leq Q < 2\,000$

- (a) $a = 16, b = 62.5$
(b) $m = 1\,000, n = 9\,000, k = -2/125$
(c) 111.98 min (d) $1\,000 < Q \leq 10\,000$

Exercise 16.3

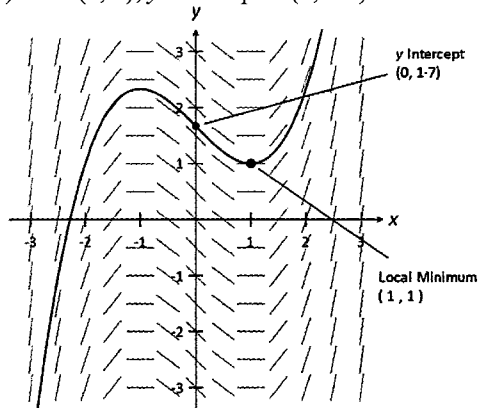
- (a) $dP/dt = 0.2P(1 - P/1000)$
 $= 0.0002P(1000 - P)$
(b) $dP/dt = 0.1P(1 - P/500)$
 $= 0.0002P(500 - P)$
(c) $dP/dt = 0.5P(1 - P/10\,000)$
 $= 0.000\,05P(10\,000 - P)$
(d) $dP/dt = 0.25P(1 - P/5000)$
 $= 0.000\,05P(5000 - P)$
- (a) $P = 1000/(1 + 19e^{-2t})$
(b) $P = 100/(1 + 4e^{-0.05t})$
(c) $C = 50/(1 + 9e^{-0.1t})$
(d) $\theta = 1000/(1 + 24e^{-0.05t})$
- (a) $y = 200/(1 + e^{-4t})$
(b) $P = 100/(1 + 9e^{-t})$
(c) $P = 50/(1 + 0.25e^{-0.2t})$
(d) $x = 100/(1 + 4e^{-0.5t})$
- (a) $P = 100/(1 + 3e^{-0.05t})$
(b) 21.97 years
- (a) $P = 20\,000/(1 + 99e^{-0.08t})$
(b) 181.2 years
- (a) $P = 2000/(1 + 199e^{-10t})$
(b) 3 weeks
- 394 minutes to reach 49.9g/L
- 11.6 days
- 15.2 hours
- Yes, if the company is able to attract about 338 families on its opening day.
- $k = 0.1099$
- $k = 0.06592$
- $dP/dt = 0.1P(1 - P/1000)$
- $y = (4e^{2t} - 3)/(3 - 2e^{2t})$

Exercise 16.4

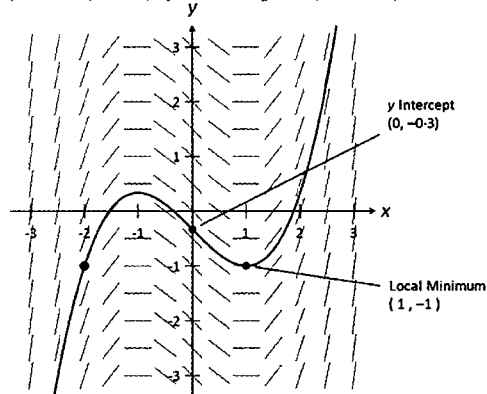
- (a) $y = \ln|x| + x^2/2 + A$
(b) $y = A(x-1) - 1$
(c) $y = \pm\sqrt{(1 - Ae^{\cos x})/x^2}$
(d) $y = Ae^{\cos x}$
- (a) $y = \sqrt{e^x + 3}$
(b) $y = \ln[(1+x)^2/2]$
(c) $y^2/2 + y = \ln(x+1) + 3/2$
(d) $y = 3xe^{x-1} - 1$ (e) $y = x$
(f) $y = \pm\sqrt{(1/\sin x - 1)}$

Exercise 16.5

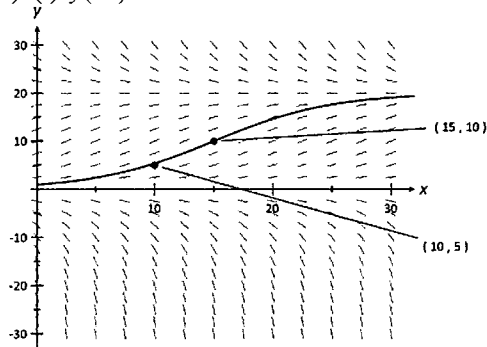
1. (a) Min (1, 1); y-intercept \approx (0, 1.7)



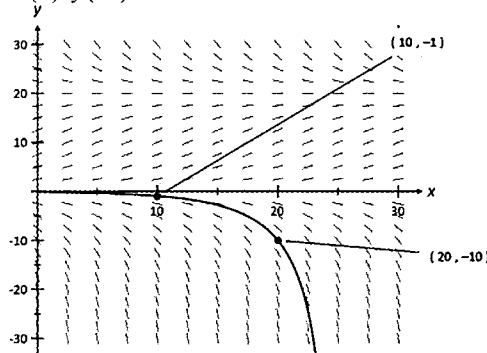
(b) Min (1, -1); y-intercept \approx (0, -0.3)



2. (a) (i) $y(10) \approx 5$

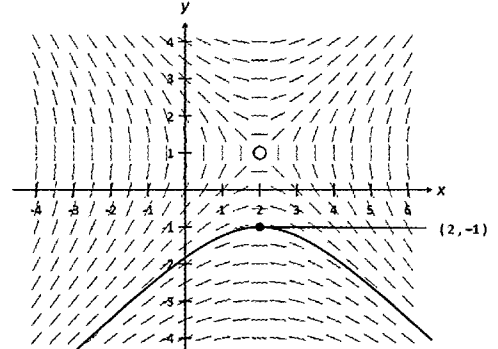


(ii) $y(10) \approx -1$

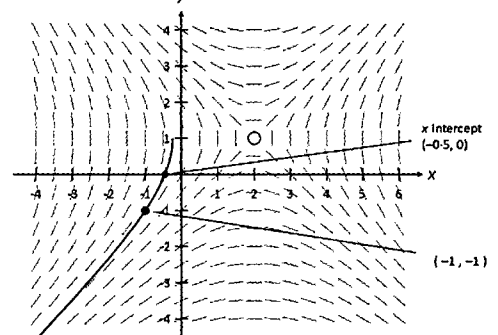


(b) $y = 0, y = 20$

3. (a) (i) Curve does not have an x-intercept.



(ii) When $y = 0, x \approx -0.5$.

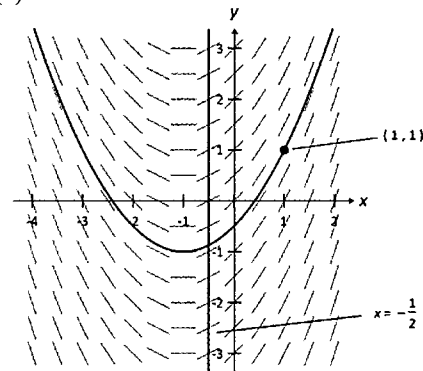


(b) $y = x - 1$ where $x \neq 2 \cap y \neq 1$

4. Slope field has zero gradient for $x = 2$ and infinite gradient for $y = 1$; hence C.

Isocline with gradient -2 is $y = -x/2 + 2$

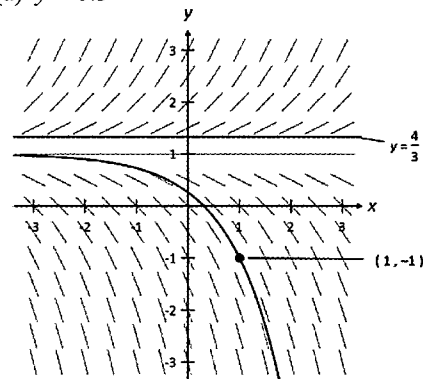
5. (a)



(b) Slope field has zero gradient for $x = -1$, hence, A.

(c) $x = -1/2$.

6. (a) $y \approx 0.3$



(b) C

(c) $y = 4/3$

7. (a) $dy/dx = 1$ (b) $dy/dx = -2$
 (c) $dy/dx = x$ (d) $dy/dx = -y$
 (e) $dy/dx = xy$ (f) $dy/dx = (x-1)/y$

Exercise 17.1

1. (a) -0.35 m (b) 0.79 s
 (c) 3.64 m (d) 3.99 m⁻¹
 2. (a) $3\pi/4$ s, -14.92 ms (b) 4.81 ms⁻¹
 3. (a) $0.4637 + (n\pi/2)$ sec. $n = 0, 1, 2, 3, \dots$
 4. (a) -8 ms (b) 2 ms⁻¹
 5. (a) $\pi/3$ s (c) $0, \pi/2, \pi$ s
 6. (a) 8 ms⁻¹ (b) $16/3$ m (c) 2 ms⁻¹
 7. (a) 0 (b) 1 sec
 8. (a) $x = -2 + 2e^{2t}$ (b) $a = 8e^{2t}$
 9. (a) -21 ms⁻² (b) $0, 2$ m
 10. (a) 4 ms⁻¹ (b) 1.76 ms⁻²
 11. (a) -2π ms⁻¹ (b) $1/2$ second
 12. (a) $9/2$ ms⁻¹ (b) $121/30$ m
 13. (a) $v = 4(1 - e^{-t})$ (b) 4 ms⁻¹
 14. (a) $v = -5(1 - e^{-2t})$ (b) -5 ms⁻¹
 15. (a) $v = (g/k)(1 - e^{-kt})$ (b) g/k
 16. $v = (5/4)\sqrt{(1 - e^{-32x})}$; $5/4$ ms⁻¹
 17. $v = 2(1 + e^{-100t})/(1 - e^{-100t})$; 2 ms⁻¹
 18. $v = \pm(1/k)\sqrt{(1 - e^{-2gk^2x})}$
 19. (a) $v = \sqrt{(16 - 9x)}$
 (b) $-4/3 \leq x \leq 4/3$; $0 \leq v \leq 4$
 20. (a) $v = 2\sqrt{(4x - x^2)}$
 (b) $0 \leq x \leq 4$; $0 \leq v \leq 4$
 21. (a) $v = 4/\sqrt{x}$ (b) $x = (6t + 64)^{2/3}$
 22. (a) $v = -2(x^2 + 1)$ (b) $x = -\tan(2t)$

Exercise 17.2

1. $x = 10 \sin 2t$ 2. $h = 5 \cos(5\pi t)$
 3. $y = 4 \sin(3t + \pi/6)$
 4. $Q = 10\sqrt{2} \sin(4\pi t - \pi/4)$
 5. (a) $x = 3 \sin(2\pi t)$ (b) 3 cm, 1 second
 (c) 6π cms⁻¹ (d) $0.05, 0.45$ seconds.
 6. (a) $x = 4 \cos(4\pi t)$ (b) 0
 (c) $\pm 8\pi\sqrt{3}$ cms⁻¹
 7. (a) $10 \sin(t + \pi/3)$ (b) $0 \leq \text{speed} \leq 10$
 (c) $\pm 5\sqrt{3}$ cm
 8. (a) 2π cms⁻¹ when $t = (2n + 1)$ sec. at $x = 0$
 (b) 0 cms⁻¹ when $t = 2n$ sec. at $x = \pm 4$ cm
 (c) 32 cm
 9. (a) $2\pi/15$ cms⁻¹; $2\pi^2/225$ cms⁻²
 (b) (i) $x = \pm\sqrt{3}$ cm (ii) $x = -1$ cm

10. (a) $\theta = 5 \sin(\pi t/12 - \pi/6)$
 (b) Min Temp 10 C at 8 pm
 (c) 16 hours
 11. (a) $h = 0.2 \cos(\pi t/14 + \pi/3)$
 (b) ± 0.14 m (c) 0.14 m
 12. (a) $x = 0.2 \sin(\pi t/14 + \pi/2) + 0.3$
 (b) (i) $-\pi/70$ (ii) 0 (c) 0.46 mg
 13. (a) (i) ± 2.27 C/hr (ii) ± 2.61 C/hr
 (b) 66.7% (c) 30 C
 14. (a) $h = 4 + 0.5 \sin(\pi t/6)$
 (b) 4.5 hours (c) 0.13 m/hour
 15. (a) $x = \pm 6\sqrt{3} \sin(\sqrt{2}t + \alpha)$
 (b) $12\sqrt{3}$ cms⁻²
 16. (b) 100 cm 17. (b) $\pm 2\pi\sqrt{105}$
 18. (a) 2 minutes, 10 (b) 2 minutes, 10
 19. (a) 2 seconds, 10 cm (b) $\pm 3\sqrt{11}$

Exercise 18.1

1. (a) $\langle 1/t, e^t, e^{-t} - te^{-t} \rangle$;
 $\langle -1/t, e, -2e^{-t} + te^{-t} \rangle$
 (b) $\langle 2 \cos 2t, -2 \sin 2t, 2(1 + \tan^2 2t) \rangle$;
 $\langle -4 \sin 2t, -4 \cos 2t, 8(1 + \tan^2 2t) \rangle$
 (c) $\langle -1/t^2, 1/(t+1)^2, -1/(t-1)^2 \rangle$;
 $\langle 2/t^3, -2/(t+1)^3, 2/(t-1)^3 \rangle$
 (d) $\langle -\pi \sin \pi t e^{\cos \pi t}, \pi \sin \pi t e^{-\cos \pi t},$
 $\frac{\pi \cos \pi t e^{\sin \pi t}}{\sin \pi t} \rangle$;
 $\langle \frac{\pi \cos \pi t e^{\cos \pi t}}{\cos \pi t}, -\frac{\pi \cos \pi t e^{-\cos \pi t}}{\cos \pi t},$
 $\frac{\pi \sin \pi t e^{-\cos \pi t}}{\sin \pi t} + \frac{\pi \cos \pi t e^{\cos \pi t}}{\sin \pi t} \rangle$
 2. $2 + 4t$; $t = -1/2$ 3. $0 \leq t \leq 2\pi$
 4. $0, \pi/2, \pi, 3\pi/2, 2\pi$ 5. $n = 4$
 6. $(2t + 4t^2)/[2\sqrt{(4 + t^2 + t^4)}]$
 7. $\{\sqrt{[5(t+1)^2 + 1]}/(t+1)\}$
 8. $4 + 6t$; 4 9. No solution
 10. $\pi/4, 3\pi/4, 5\pi/4, 7\pi/4$
 11. (a) $\langle a, 2 \sin t, 3 \cos t \rangle + c$; $\langle 0, 2, -3 \rangle$
 (b) $\langle t + \ln t, t - \ln t, \ln(1+t) \rangle + c$;
 $\langle 1 + \ln 2, 1 - \ln 2, \ln(3/2) \rangle$
 12. (a) $\sqrt{2}, \pi/2$ (b) $\sqrt{5}, 2.64$
 13. $\langle t - t^2 + 1, 4t + 1, t/2 \rangle$
 14. $\langle \cos \pi t, t, -1 + 2 \sin \pi t \rangle$
 15. $\langle -1, t, -t \rangle$
 16. $\langle -\sin \pi t, 1 - \cos \pi t, \pi t - \sin \pi t \rangle$
 17. 50

Exercise 18.2

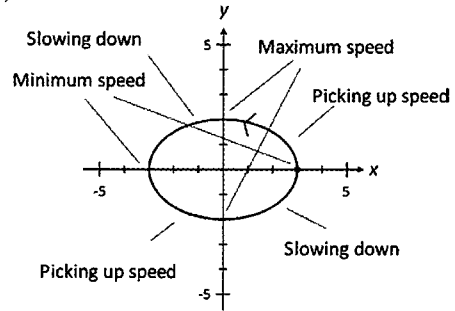
1. (a) $\langle 10, 20, -8 \rangle$ (b) $\langle -8, 18, 34 \rangle$
 (c) $\langle 0, 0, 1 + \ln 2 \rangle$ (d) $\langle 0, 1, \pi/4 \rangle$

2. (a) $\langle 7, -4, 150 \rangle$ (b) $\langle -101, 99, 22 \rangle$
 (c) $\langle 1 + 6\pi, 1 + 2\pi, -2\pi \rangle$
 (d) $\langle 8\pi - 1, 1, 8\pi \rangle$
3. (a) $\langle 0, 0, 2 \rangle$; $\sqrt{10} \text{ ms}^{-1}$
 (b) 0° (d) 3.05 m
4. (b) 45° , 1 ms^{-1} (c) $\langle 0, 0, 0 \rangle$
5. (a) 1 sec. (b) 0.54 m
 (c) 1 sec.
6. (a) Min of 0 cm when $t = 2n\pi$ sec.
 Max of $2\sqrt{2} \text{ cms}^{-1}$ when $t = (2n + 1)\pi$ sec.
 (b) $t = 0, \pi/2, \pi, 3\pi/2, 2\pi$ sec.
7. (b) $x - 1 = 2 - y = z - 1$
8. (a) 143.3° (b) 2 s, $\langle -16/3, 3, -2 \rangle$
 (c) $x = t/3 - 4t, y = t + 1, z = -2t + 2$
9. (a) $t = 2$ sec. at $\langle 0, -4, 8 \rangle$
 (b) 17.1°
10. (a) $t = 1$ sec. at $\langle 2, 0, 0 \rangle$
 (b) 10.89°

Exercise 18.3

1. P: $0\mathbf{i} + 2\mathbf{j}$, $x^2 + y^2 = 4$ clockwise;
 Q: $2\mathbf{i}$, $x^2 + y^2 = 4$ anti-clockwise
 R: $2\mathbf{i}$, $x^2 + y^2 = 4$ clockwise
2. (a) In the direction of the positive y -axis;
 $2\pi/3$ to the positive x -axis
 (b) $-\pi\mathbf{j}$ (c) $1/2$
3. (a) 1
 (b) $x^2 + y^2 = 1/(16\pi^2)$; anti-clockwise
 (d) 1
4. $\mathbf{a} \cdot \mathbf{v} = 0$ for all t .
5. (a) $-i$ (b) $4\pi^2 i$
 (c) $t = (4n + 3)/8$ sec. for $n = 0, 1, 2, 3, \dots$
6. (a) \mathbf{j} (b) $(-\pi/4)\mathbf{j}$
 (c) $t = (6n + 2)/3$ sec. for $n = 0, 1, 2, 3, \dots$
7. (a) $t = n\pi$ sec. for $n = 0, 1, 2, 3, \dots$
 (b) $(n + 1/6)\pi$ sec. for $n = 0, 1, 2, 3, \dots$
 (c) $x^2 + (y - 2)^2 = 1$; clockwise
8. (a) $x^2 + y^2 = 1$; anti-clockwise
 (b) $\sqrt{2}\mathbf{i} + \sqrt{2}\mathbf{j}$ or $-\sqrt{2}\mathbf{i} - \sqrt{2}\mathbf{j}$
 (c) $t = (4n + 1)\pi/8$ sec. for $n = 0, 1, 2, 3, \dots$
9. No collision
10. (a) $0, \pi/2, \pi, 3\pi/2, 2\pi$
 (b) $\sqrt{(9 - 5 \cos t)}$
 (c) Max speed = 3 when $t = \pi/2$ at $(0, 2)$,
 and $t = 3\pi/2$ at $(0, -2)$;
 Min speed = 2 when $t = 0$ & 2π at $(3, 0)$
 and $t = \pi$ at $(-3, 0)$.

10. (d)



11. (a) 2π (b) $0, \pi/2, \pi, 3\pi/2, 2\pi$
 (c) At $(0, -4)$ when $t = (4n + 1)\pi/2, -3\mathbf{i}$;
 At $(0, 4)$ when $t = (4n + 3)\pi/2, 3\mathbf{i}$;
 (d) At $(3, 0)$ when $t = 2n\pi, -4\mathbf{j}$;
 At $(-3, 0)$ when $t = (2n + 1)\pi, 4\mathbf{j}$;
12. Period 2π ; $(x - 2)^2/9 + (y - 4)^2/25 = 1$
13. (a) 3 m (b) $\pm 12\pi i$
 (c) $t = n/2$ sec. for $n = 0, 1, 2, 3, \dots$
 (d) $t = (4n + 3)/8$ sec. for $n = 0, 1, 2, 3, \dots$
14. (a) $13\sqrt{2}/2 \text{ cm}$
 (b) $x^2/25 + y^2/144 = 1$, clockwise
 (c) $\mathbf{r} = 5\mathbf{i}$ for $t = 2n$ sec. for $n = 0, 1, 2, 3, \dots$
 $\mathbf{r} = -5\mathbf{i}$ for $t = (2n + 1)$ sec. $n = 0, 1, 2, 3, \dots$
 (d) $t = (6n + 5)/6$ sec. for $n = 0, 1, 2, 3, \dots$
15. (a) Min 3 cms^{-1} , Max 4 cms^{-1}
 (b) $\pm 3\mathbf{i}$ or $\pm 4\mathbf{j}$
 (c) $t = n\pi$ sec. for $n = 0, 1, 2, 3, \dots$
16. (a) $(x - 1)^2/9 + (y - 2)^2/16 = 1$, anti-clockwise
 (b) $2\sqrt{5} \text{ cm}$ or $\sqrt{37} \text{ cm}$ or $2\sqrt{2} \text{ cm}$ or $\sqrt{5} \text{ cm}$
17. $t = 0.64$ sec. at $(-2.4, 2.4)$, $\mathbf{v}_P = 1.8\mathbf{i} + 3.2\mathbf{j}$,
 $\mathbf{v}_Q = -1.2\mathbf{i} - 0.8\mathbf{j}$
18. When $t = \pi$ sec at $(1, -2)$; π radians

Exercise 18.4

1. (a) $30\mathbf{i} + (30\sqrt{3} - 9.8t)\mathbf{j}$, 5.6° to the horizontal
 (b) 95.6° (c) 10.60 sec., 318 m
2. (a) $106.07\mathbf{i} + 61.97\mathbf{j}$ (b) 20.7°
 (c) 1.93 s, 5.28 s (d) $y = x - 0.0392x^2$
3. (a) $\langle 20t, 20t - 4.9t^2 \rangle$
 (b) 45°
 (c) $\langle 17.25, 13.61 \rangle$ when $t = 0.86$ sec.
 (d) 93.7 m
4. (a) $\langle 25\sqrt{3}, 25 - 9.8t \rangle$;
 $\langle 25\sqrt{3}t, 25t - 4.9t^2 + 150 \rangle$
 (b) 8.64 sec.
 (c) -54° to the horizontal
 (d) 374.3 m
5. (a) $\langle 50, -9.8t \rangle$; $\langle 50t, (100 - 4.9t^2) \rangle$
 (b) 4.52 sec. (c) 225.88 m
 (d) -41.52° to the horizontal

6. (a) 13 ms^{-1} (b) 2.975 m
 (c) 2.75 m
 (d) 9.52 ms^{-1} , -58.31° to the horizontal
7. (a) $p = 30t_0$, $q = (30\sqrt{3})t_0 - 4.9t_0^2$
 (b) 7.07 sec.
 (c) 244.90 m up the slope of the hill
8. (a) $y = x \tan(20^\circ) - 4.9x^2/[400 \cos^2(20^\circ)]$
 or $y = -0.0139x^2 + 0.364x$
 (b) 18.89 m (c) 19.10 m
 (d) $t = 0 \text{ sec}$
9. (a) $\langle 8.09, -18.62 \rangle$ (b) 20.30 m
 (c) 20.34 m (d) 11.5°
10. (a) 4 sec. (b) $\langle 72, 17.6 \rangle$
11. $20 \text{ sec.}; 40\sqrt{5} \text{ m}$ 12. (b) $3/10$
13. (a) $\langle 3t - 2, 2t \rangle$ (b) $\langle 6t, 2 \rangle$
 (c) $0, 2/3$
14. (a) $\langle 20, 10 \rangle$ (b) 5
 (c) 106.89
15. (a) 48.01° above the horizontal
 (b) 26.9 m (c) 20 m when $t = 2 \text{ sec.}$
 (d) $\langle 32, 0 \rangle$ when $t = 4 \text{ sec.}$
16. (a) 14 m (b) $\langle 14, 10 \rangle$
 (c) 17.20 m (d) 20.34 m

Exercise 19.1

1. (a) $\bar{X} \sim N(100, 12^2/20)$
 (b) 0.3385 (c) 0.0312
2. (a) $\bar{X} \sim N(72, 8^2/50)$
 (b) 0.0987 (c) 0.4615
3. (a) $n = 74$ (b) $70 \leq n \leq 79$
4. (a) $n = 25$ (b) $25 < n < 100$
5. (a) 3 (b) $\mu = 3, \sigma = (\sqrt{3})/7$
 (c) $3 < n < 12$
6. (a) 18 (b) $\mu = 18, \sigma = 2/\sqrt{3}$
 (c) $48 < n < 108$
7. (a) Since, $X \sim \text{Normal}$, $\bar{X} \sim N(1.7, 0.026^2)$
 (b) 0.6497 (c) 0.9728
8. (a) Since, $X \sim \text{Normal}$,
 $\bar{X} \sim N(875, 11.7^2/\sqrt{20})$
 (b) 0.3346 (c) 0.0280
 (d) $n \geq 61$
9. (a) Since, $X \sim \text{Normal}$, $\bar{X} \sim N(175, 8.5206^2)$
 (b) $n = 90$ (c) 8
 (d) 1812
10. (a) Since, $X \sim \text{Normal}$, $\bar{X} \sim N(163, 9.8387^2)$
 (b) $n = 67$ (c) 35
 (d) 162
11. (a) $15, (\sqrt{42})/2; 15, (\sqrt{42})/10$
 (b) $5 \leq k \leq 10$
12. (a) $95, (\sqrt{19})/2; 95, (\sqrt{19})/12$
 (b) $3 \leq k \leq 18$
13. (a) $0.6, (\sqrt{57})/10$ (b) $0.6, (\sqrt{19})/20$

14. (a) $P(X=x) = 1/8$ $x = 1, 2, 3, \dots, 7, 8$
 $\mu = 4.5, \sigma = 2.2913$
 (b) $4.5, 0.3819$
15. (a) $P(X=x) = 1/6$ $x = 1, 2, 3, 4, 5, 6$
 $\mu = 3.5, \sigma = 1.7078$
 (b) $3.5, 0.4270$ (c) $19 \leq n \leq 291$

Exercise 19.2

1. (a) $\bar{X} \sim N(200, 35^2/60)$ (b) 0.9866
2. (a) $\bar{X} \sim N(4.5, 1.2^2/80)$ (b) 0.5439
3. (a) $\bar{X} \sim N(12, 4/3)$ (b) $1/12$ (c) 0.6135
4. (a) $\bar{X} \sim N(28, 108/49)$
 (b) (i) $1/18$ (ii) 0.4110 (c) $n \geq 82$
5. (a) 12 min (b) $\bar{X} \sim N(12, 49/90)$
 (c) (i) $3/7$ (ii) 0.08767 (d) 0.1660
6. (a) If $n < 30$, distribution for \bar{X} is not known,
 mean = 2 , s.d. = $(\sqrt{3})/(15\sqrt{n})$.
 If $n \geq 30$, by the CLT, $\bar{X} \sim \text{Normal}$
 mean = 2 , s.d. = $(\sqrt{3})/(15\sqrt{n})$.
 (b) (i) 0.6824 (ii) 0.8068
 The prob. of an event occurring increases
 as sample size n increases.
 (c) $n \geq 134$ (d) 0.9145
7. (a) (i) 0.8286 (ii) 0.9584 (b) $n = 240$
8. (a) (i) 0.7558 (ii) 0.8364 (b) 127.4 min.
9. (a) (i) 0.4115 (ii) 0.4718 (b) 87.2 min.
10. (a) $\bar{X} \sim N(0.15, 51/2000)$ (b) 0.1490
 (c) 29
11. (a) $\bar{X} \sim N(11/2, 33/200)$
 (b) (i) $3/10$ (ii) 0.8907 (c) 89
12. (a) $\bar{X} \sim N(7, 91/1000)$
 (b) (i) 0.3556 (ii) 0.4995 (c) 50
13. (a) $P(X=x) = 1/8$ for $x = 1, 2, 3, \dots, 7, 8$
 (b) $\bar{X} \sim N(9/2, 7/48)$ (c) 0.9048 (d) 0.7042
14. (a) $P(X=x) = 1/6$ for $x = 1, 2, 3, 4, 5, 6$
 Mean = $7/2$
 (b) $\bar{X} \sim N(7/2, 5/84)$ (c) 0.0202 (d) $n \geq 12$
15. (a) $5, 3(\sqrt{2})/2$ (b) $5, 3/10$
 (c) 0.9044 (d) 0.6408
16. (a) $P(X=x) = \frac{\binom{7}{x} \binom{3}{3-x}}{\binom{10}{3}}$ for $x = 0, 1, 2, 3$
 Mean = $21/10$
 (b) $\bar{X} \sim N(21/10, 49/5000)$ (c) 0.1562

Exercise 19.3

1. (a) $\bar{X} \sim N(20, 0.3^2)$ (b) $N(20, 0.3^2)$
2. (a) $\bar{X} \sim N(100, (7\sqrt{2}/10)^2)$
 (b) $N(100, (7\sqrt{2}/10)^2)$
3. $\bar{X} \sim N(50, 1/2)$
4. (a) $\bar{X} \sim N(3, 9/400)$ (b) $N(3, 9/400)$
5. (a) $\bar{X} \sim N(2, 1/250)$ (b) $N(2, 1/250)$

6. (a) $15, (5\sqrt{3})/3$ (b) $\bar{X} \sim N(15, 5/48)$
 (b) $N(15, 5/48)$
 7. (a) $0, (\sqrt{15})/5$ (b) $N(0, 1/200)$

Exercise 20.1

1. (a) 59.54, 5.7844 (b) 59.54, 5.7844
 2. (a) 13.5, 8.7115 (b) $N(13.5, 1.1246^2)$
 3. $\bar{X} \sim N(100, 9/8)$; $N(100, 9/8)$
 4. $\bar{X} \sim N(10, 1/5000)$; $N(10, 1/5000)$
 5. (a) $1, (\sqrt{30})/6$; $\bar{X} \sim N(1, (\sqrt{30}/60)^2)$
 (b) $N(0, 1)$
 6. (a) $5, (5\sqrt{3})/3$; $\bar{X} \sim N(5, (\sqrt{3}/6)^2)$
 (b) $N(0, 1)$; approx. $N(0, 1)$
 7. (a) 1.1, 0.9434, 0.9595
 (b) 0.5708
 8. (a) 11.4, 5.1743, 5.2628
 (b) 0.9367

Exercise 20.2

1. (a) $\bar{X} \sim N(33.7, 1.0733^2)$
 (b) (i) 33.7 ± 2.76 (ii) 33.7 ± 1.88
 (c) $n \geq 23$
 2. (a) $\bar{X} \sim N(201.4, 3.525^2)$
 (b) (i) 201.4 ± 5.80 (ii) 201.4 ± 7.65
 (c) $n \geq 48$
 3. (a) $\bar{X} \sim N(5.4, 0.12^2)$
 (b) (i) 5.4 ± 0.24 (ii) 5.4 ± 0.34
 (c) $n \geq 98$
 4. (a) (i) 20.7 ± 0.57 (ii) 20.7 ± 1.14
 (b) $n \geq 46$
 5. (a) (i) 0.3341 (ii) 0.01606
 (b) (i) 485 ± 5.76 (ii) 485 ± 6.13
 (c) $n \geq 25$
 6. (a) 0.9431 (b) 125 ± 4.89 (c) $n \geq 28$
 7. (a) 0.1030 (b) 12 ± 1.55 (c) 79.4%
 8. (a) 0.9605 (b) 2.5 ± 0.089 (c) 88.6%
 9. (a) 183 ± 1.18 (b) 90.4% (c) $n \geq 60$
 10. (a) 1.645 (b) $29.8 \leq \mu \leq 30.2$
 11. (a) $9.993 \leq \mu \leq 10.007$
 $9.991 \leq \mu \leq 10.009$
 $9.988 \leq \mu \leq 10.012$
 (b) No cause.
 12. (a) $999.81 \leq \mu \leq 1000.19$
 $999.77 \leq \mu \leq 1000.23$
 $999.70 \leq \mu \leq 1000.3$
 (b) No cause.

Exercise 20.3

1. Significant at 10%, 5% and 1% levels.
 2. Significant at 10% and 5% but not at 1%.
 3. Significant at 10%, 8% and 2% levels.
 4. (a) Significant at 5% level.
 (b) 15.7%
 5. (a) 5.9% (b) (i) $n \geq 55$ (ii) $n \geq 39$
 6. (a) 2.5% (b) (i) $n \geq 107$ (ii) $n \geq 62$

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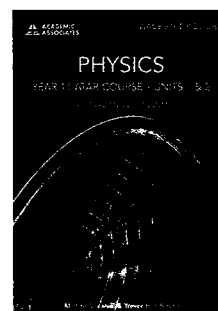
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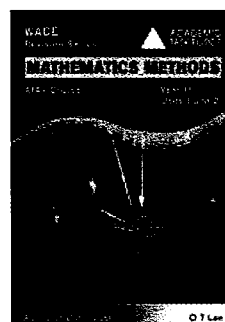
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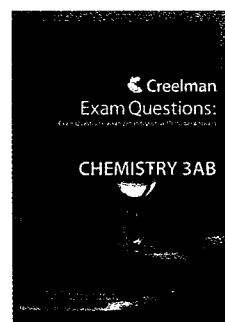
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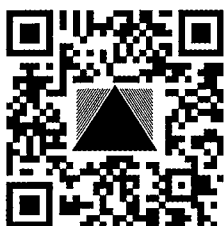
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